

**Answer Key**

1(a)  $y = \frac{3}{4}x + 4$  (c)  $y = -\frac{4}{3}x - 10$

(d) Since gradient of line  $h$  = gradient of line  $l$ , the lines are parallel and do not intersect.

2(a)(i)  $a = -3, b = 5, c = 9$  (a)(ii)  $4n - 7$

2(b)(i) 4<sup>th</sup> line:  $\frac{1}{4} - \frac{1}{5} = \frac{1}{20}$ ; 5<sup>th</sup> line:  $\frac{1}{5} - \frac{1}{6} = \frac{1}{30}$  (b)(ii)  $n^{\text{th}}$  line:  $\frac{1}{n} - \frac{1}{n+1} = \frac{1}{n(n+1)}$

(b)(iii) Since  $n$  is not an integer, he is not correct. (b)(iv)  $1 = \frac{1}{2} + \frac{1}{6} + \frac{1}{7} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \frac{1}{42}$

3(a)  $\mathbf{A} = \begin{pmatrix} 390 & 300 & 350 \\ 150 & 200 & 180 \end{pmatrix}$  (b)  $\mathbf{H} = (0.15 \quad 0.45)$  (c)(i)  $\mathbf{R} = \begin{pmatrix} 610 & 550 & 550 \\ 410 & 430 & 350 \end{pmatrix}$

(c)(ii)  $\mathbf{M} = \begin{pmatrix} 1710 \\ 1190 \end{pmatrix}$

(c)(iii) The elements represent the **total weight of** newspapers and clothes collected **respectively** by the 3 classes, from the **2 collections / weeks**.

(c)(iv) \$792

4(a)  $\frac{500}{x}$  (b)  $\$(x+1)\left(\frac{500}{x} - 3\right)$  (d)  $x = 9.63$  or  $-17.30$  (e) 49

5(a)  $p = 15$  (c) 34 (d)  $-0.15$  (e)(ii) Any integer value of  $17 \leq x \leq 73$

6(c) \$1391 (d)  $806 \text{ m}^3$

7(b) 1520 m (c)  $076.2^\circ$  (d) 1420 m (e) 164 m

8(a)(i)  $15^\circ$  (ii)  $75^\circ$  (iii)  $105^\circ$  (iv)  $15^\circ$  (b) On the circle

(c) False.

9(a)(i)

| Test | Lower Quartile | Median    | Upper Quartile | Interquartile range |
|------|----------------|-----------|----------------|---------------------|
| 1    | <b>24</b>      | 30        | <b>37</b>      | <b>13</b>           |
| 2    | 20             | <b>35</b> | 45             | 25                  |

(a)(ii) 45 (iii) Disagree. (b)(i) 56.1 km/h (b)(ii) 9.98

10(a) Height of small cup = 9.9 cm, height of medium cup = 12.4 cm

(b) 393 ml (c) She is not correct.

## Mathematics Paper 1 Solutions (Prelim 2020)

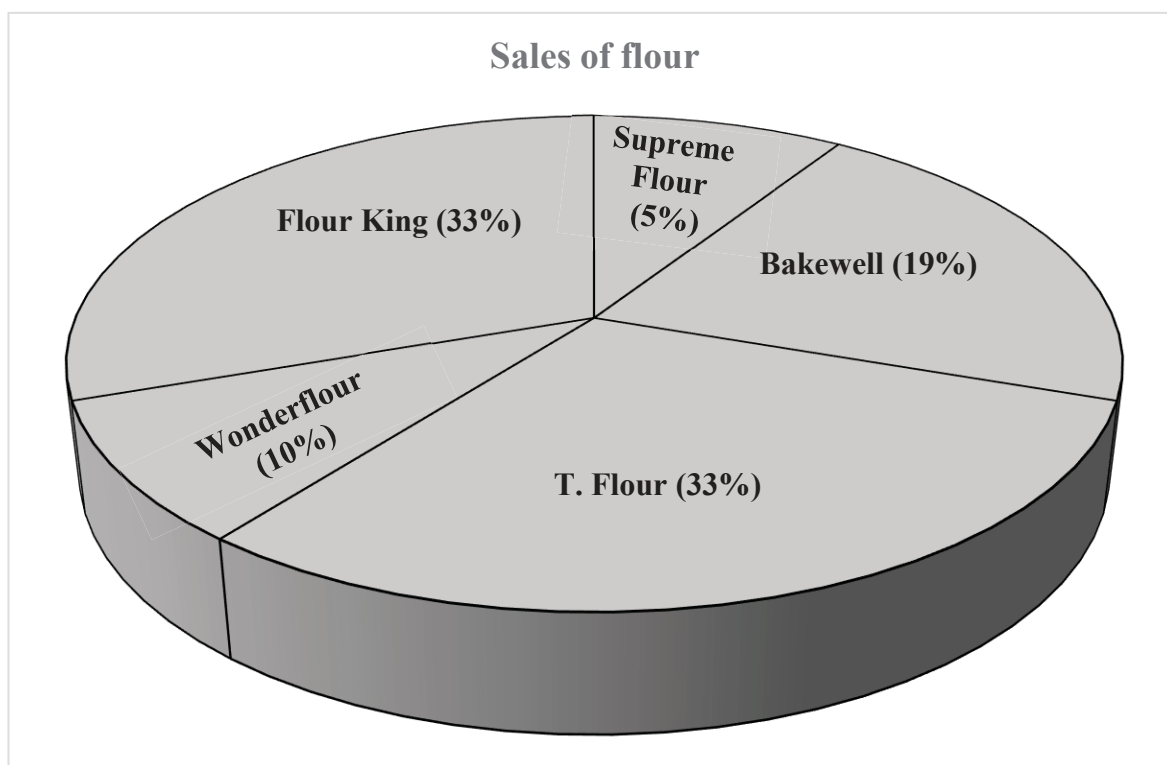
Answer **all** the questions.

- 1 Write the following in order of the size, starting with the **smallest**.

$$\frac{23}{45} \quad \sqrt[3]{-64} \quad (-0.86)^2 \quad -0.7^2$$

$$\text{Answer } \sqrt[3]{-64}, -0.7^2, \frac{23}{45}, (-0.86)^2 \quad [1]$$

- 2 The following pie chart represents the percentage of the sales of five different brands of flour in a supermarket.



Explain how the chart above may be misleading.

The **3D presentation** of the pie-chart makes it seem like T. Flour holds the largest proportion of the pie chart, and hence the largest percentage of sales, **when in actual fact** is equal to Flour King at 33%.

[1]

- 3 (a) Simplify  $\left(\frac{p^6}{q^3}\right)^{-\frac{2}{3}}$ , leaving your answer in positive indices.

$$\begin{aligned}\left(\frac{p^6}{q^3}\right)^{-\frac{2}{3}} &= \frac{p^{-4}}{q^{-2}} \\ &= \frac{q^2}{p^4}\end{aligned}$$

Answer .....  $\frac{q^2}{p^4}$  [2]

- (b) Given that  $8^{1+b} = 16^{b-2}$ , find the value of  $b$ .

$$\begin{aligned}8^{1+b} &= 16^{b-2} \\ 2^{3(1+b)} &= 2^{4(b-2)}\end{aligned}$$

Comparing powers,

$$\begin{aligned}3(1+b) &= 4(b-2) \\ 3+3b &= 4b-8 \\ -b &= -11 \\ b &= 11\end{aligned}$$

Answer  $b =$  ..... 11 [2]

- 4 (a) Calculate  $\frac{18.6^3}{\sqrt{23}-2.59}$ .

Write down the first five digits of your answer.

Answer ..... 2917.2 [1]

- (b) Write your answer to **part (a)** correct to 2 significant figures.

Answer ..... 2900 [1]

- 5 Factorise  $5qr + 6s - 2r - 15qs$  completely.

$$\begin{aligned}5qr + 6s - 2r - 15qs &= 5qr - 15qs + 6s - 2r \\ &= 5q(r - 3s) - 2(r - 3s) \\ &= (5q - 2)(r - 3s)\end{aligned}$$

Answer .....  $(5q - 2)(r - 3s)$  [2]

- 6 The area of an  $8 \text{ km}^2$  park is represented on a map by an area of  $200 \text{ cm}^2$ .

(a) If the map has a scale of  $1:n$ , find the value of  $n$ .

**Area scale**

Map : Actual

$$200 \text{ cm}^2 : 8 \text{ km}^2$$

$$1 \text{ cm}^2 : 0.04 \text{ km}^2$$

**Length scale**

Map : Actual

$$\sqrt{1 \text{ cm}^2} : \sqrt{0.04 \text{ km}^2}$$

$$1 \text{ cm} : 0.2 \text{ km}$$

$$1 \text{ cm} : 0.2 \times 1000 \times 100 \text{ cm}$$

$$1 : 20\,000$$

$$\text{Answer } n = \frac{20\,000}{\dots\dots\dots} [2]$$

(b) If the perimeter of the park on the map is  $13 \text{ cm}$ , calculate the actual perimeter in kilometres.

$$\begin{aligned} \text{Actual perimeter} &= 13 \times 0.2 \\ &= 2.6 \text{ km} \end{aligned}$$

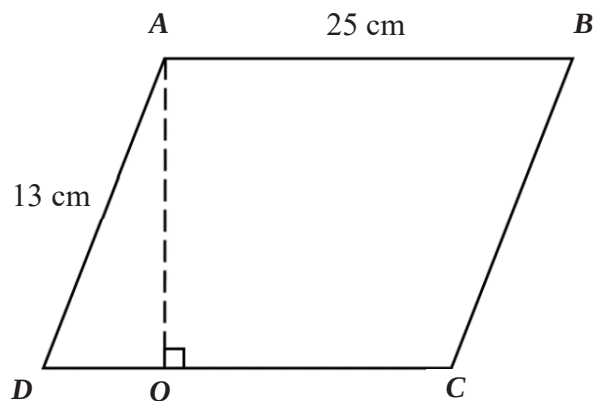
$$\text{Answer } \frac{2.6}{\dots\dots\dots} \text{ km} [1]$$

(c) A renovation was done on the park and its area on the map is now represented by the following parallelogram  $ABCD$ , with  $AB = 25 \text{ cm}$ ,  $AD = 13 \text{ cm}$  and  $DO = \frac{1}{5} DC$ . Find the percentage change in the area of the park.

$$\begin{aligned} DO &= \frac{1}{5} \times 25 \\ &= 5 \text{ cm} \end{aligned}$$

By Pythagoras' Theorem,

$$\begin{aligned} AO &= \sqrt{13^2 - 5^2} \\ &= 12 \text{ cm} \end{aligned}$$



$$\begin{aligned} \text{Area of parallelogram} &= 12 \times 25 \\ &= 300 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Percentage change} &= \frac{300 - 200}{200} \times 100\% \\ &= 50\% \end{aligned}$$

$$\text{Answer } \frac{50\%}{\dots\dots\dots} [3]$$

- 7 Write as a single fraction in its simplest form  $\frac{5x}{1-x^2} + \frac{3}{x-1}$ .

$$\begin{aligned}\frac{5x}{1-x^2} + \frac{3}{x-1} &= \frac{5x}{(1+x)(1-x)} + \frac{3}{x-1} \\ &= \frac{5x}{(1+x)(1-x)} - \frac{3}{1-x} \\ &= \frac{5x-3(1+x)}{(1+x)(1-x)} \\ &= \frac{5x-3-3x}{(1+x)(1-x)} \\ &= \frac{2x-3}{(1+x)(1-x)}\end{aligned}$$

$$\text{Answer } \frac{2x-3}{(1+x)(1-x)} \dots\dots\dots [3]$$

- 8 Without using a calculator, show that  $5^{2018} - 5^{2017}$  is an even number.

Answer

$$\begin{aligned}5^{2018} - 5^{2017} &= 5^{2017}(5-1) \\ &= 5^{2017} \times 4\end{aligned}$$

**Option 1:** Since 4 is an even factor of  $5^{2018} - 5^{2017}$ ,  $5^{2018} - 5^{2017}$  is an even number.

**Option 2:** Since  $5^{2018} - 5^{2017}$  is a multiple of 4, which is an even number,  $5^{2018} - 5^{2017}$  is an even number.

**Option 3:** Since 4 is an even number, and an even number multiplied by any number is even,  $5^{2018} - 5^{2017}$  is an even number.

[2]

- 9 Written as a product of its prime factors,  $3024 = 2^x \times 3^y \times 7$ .

(a) Find the values of  $x$  and  $y$ .

$$\begin{aligned} \text{Answer } x &= \dots\dots\dots 4 \\ y &= \dots\dots\dots 3 \quad [2] \end{aligned}$$

(b) Explain if 3024 is a square number.

**Answer Since the powers of the prime factors of 3024 are not even (multiples of 2), 3024 is not a square number. OR 3024 is not a square number as it cannot be expressed as a product of 2 identical integers. [1]**

- 10 A cylindrical container has a radius of 5.4 cm and a capacity of 1.8 litres.  
Calculate the height of the container.

$$\begin{aligned} 1.8 \text{ litres} &= 1800 \text{ ml} \\ &= 1800 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Height} &= 1800 \div \pi(5.4)^2 \\ &= 19.648\dots \text{ cm} \\ &= 19.6 \text{ cm (3sf)} \end{aligned}$$

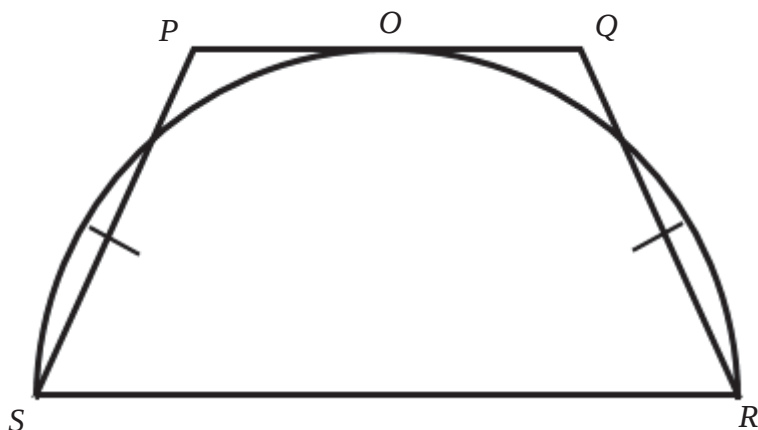
$$\text{Answer } \dots\dots\dots 19.6 \text{ cm } [2]$$

- 11 Solve the equation  $\frac{2x-3}{3} - \frac{x+2}{5} = 4$ .

$$\begin{aligned} \frac{2x-3}{3} - \frac{x+2}{5} &= 4 \\ \frac{5(2x-3) - 3(x+2)}{15} &= 4 \\ 10x - 15 - 3x - 6 &= 60 \\ 7x - 21 &= 60 \\ 7x &= 81 \\ x &= 11\frac{4}{7} \end{aligned}$$

$$\text{Answer } x = \dots\dots\dots 11\frac{4}{7} \quad [2]$$

- 12 The following diagram shows a semicircle  $ROS$  and an isosceles trapezium  $PQRS$ , where  $PS = (2x + 2y)$  cm,  $QR = (3y - 2x + 5)$  cm,  $RS = (5y + x - 1)$  cm. Given that  $PS = QR$  and that the height of the trapezium is  $(x + 2y)$  cm, find the exact area of the semicircle  $ROS$ , giving your answer in terms of  $\pi$ .



$$2x + 2y = 3y - 2x + 5$$

$$4x - y = 5 \text{ ----- (1)}$$

$$2(x + 2y) = 5y + x - 1$$

$$2x + 4y = 5y + x - 1$$

$$x - y = -1 \text{ ----- (2)}$$

$$(1) - (2):$$

$$3x = 6$$

$$x = 2$$

Sub.  $x = 2$  into (2).

$$2 - y = -1$$

$$-y = -3$$

$$y = 3$$

$$\text{Radius of semicircle} = 2 + 2(3)$$

$$= 8 \text{ cm}$$

$$\text{Area of semicircle} = \frac{1}{2} \pi (8)^2$$

$$= 32\pi \text{ cm}^2$$

Answer .....  $32\pi$  .....  $\text{cm}^2$  [4]

- 13 Mrs Lai would like to deposit \$1080 in a bank which pays 7 % interest per annum compounded half-yearly. Calculate the amount of money in the account at the end of 2 years.

$$\begin{aligned}\text{Total} &= P \left( 1 + \frac{r}{100} \right)^n \\ &= 1080 \left( 1 + \frac{\frac{7}{2}}{100} \right)^4 \\ &= \$1239.32 \text{ (nearest cents)}\end{aligned}$$

Answer \$ .....1239.32..... [2]

- 14 5 men are hired to paint a house. If an additional man is hired, the painting can be completed 4 days earlier. Calculate the number of additional men to be hired if the painting is to be completed 18 days earlier.

Let the number of men be  $m$  and the number of days be  $d$ .

$$\begin{aligned}m &\propto \frac{1}{d} \\ m &= \frac{k}{d}, \text{ where } k \text{ is a non-zero constant}\end{aligned}$$

$$\begin{aligned}\text{When } m &= 5, \\ 5 &= \frac{k}{d} \\ k &= 5d \text{ --- (1)}\end{aligned}$$

$$\begin{aligned}\text{When } m &= 6, \\ 6 &= \frac{k}{d-4} \text{ --- (2)}\end{aligned}$$

Sub (1) into (2).

$$\begin{aligned}6 &= \frac{5d}{d-4} \\ 6d - 24 &= 5d \\ d &= 24\end{aligned}$$

$$\text{When } d = 24 - 18 = 6,$$

$$m = \frac{k}{6}$$

$$\begin{aligned}k &= 5d \\ &= 5(24) \\ &= 120\end{aligned}$$

$$\begin{aligned}m &= \frac{120}{6} \\ &= 20\end{aligned}$$

$$\begin{aligned}\text{Additional number of men} &= 20 - 5 \\ &= 15\end{aligned}$$

Answer .....15..... [3]

- 15 A polygon has  $n$  sides. Two of its exterior angles are  $24^\circ$  and  $86^\circ$ , while the other  $(n-2)$  exterior angles are  $50^\circ$  each. Calculate the value of  $n$ .

$$24^\circ + 86^\circ + 50^\circ(n-2) = 360^\circ$$

$$110 + 50n - 100 = 360$$

$$50n = 350$$

$$n = 7$$

Answer  $n = \overset{7}{\dots\dots\dots}$  [2]

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- 16 The table below shows the number of enrichment lessons attended by students.

|                    |   |   |     |   |   |   |
|--------------------|---|---|-----|---|---|---|
| Number of lessons  | 0 | 1 | 2   | 3 | 4 | 5 |
| Number of students | 1 | 3 | $x$ | 8 | 5 | 2 |

- (a) Write down the largest possible value of  $x$  given that 3 is the only mode.

Answer  $x = \overset{7}{\dots\dots\dots}$  [1]

- (b) Write down the largest possible value of  $x$  given that the median is 3.

Answer  $x = \overset{10}{\dots\dots\dots}$  [1]

- (c) Calculate the value of  $x$  given that the mean is 2.5.

$$\frac{0(1) + 1(3) + 2x + 3(8) + 4(5) + 5(2)}{19 + x} = 2.5$$

$$\frac{57 + 2x}{19 + x} = 2.5$$

$$57 + 2x = 47.5 + 2.5x$$

$$-0.5x = -9.5$$

$$x = 19$$

Answer  $x = \overset{19}{\dots\dots\dots}$  [2]

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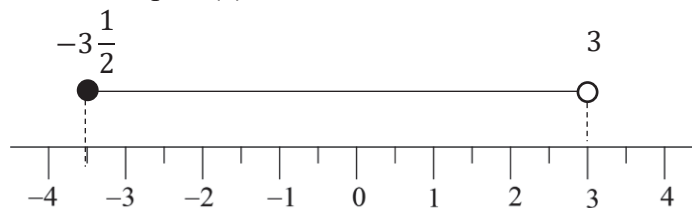
- 17 (a) Solve the inequalities  $x - 9 \leq 3x - 2 < \frac{2}{3}x + 5$ .

$$x - 9 \leq 3x - 2 \text{ and } 3x - 2 < \frac{2}{3}x + 5$$

$$\begin{array}{ll} x - 9 \leq 3x - 2 & 3x - 2 < \frac{2}{3}x + 5 \\ -2x \leq 7 & 2\frac{1}{3}x < 7 \\ x \geq -3\frac{1}{2} & x < 3 \end{array}$$

Answer  $-3\frac{1}{2} \leq x < 3$  [2]

- (b) Represent your answer to part (a) on the number line below.



[1]

18 Given that  $5y = \sqrt{\frac{6 + xz^2}{x}}$ ,

- (a) find the value of  $y$  when  $x = 2$  and  $z = -1$ .

$$\begin{aligned} 5y &= \sqrt{\frac{6 + 2(-1)^2}{2}} \\ 5y &= 2 \\ y &= \frac{2}{5} \end{aligned}$$

Answer  $y = \frac{2}{5}$  [2]

- (b) express  $x$  in terms of  $y$  and  $z$ .

$$\begin{aligned} 25y^2 &= \frac{6 + xz^2}{x} \\ 25xy^2 &= 6 + xz^2 \\ 25xy^2 - xz^2 &= 6 \\ x(25y^2 - z^2) &= 6 \\ x &= \frac{6}{25y^2 - z^2} \end{aligned}$$

Answer  $x = \frac{6}{25y^2 - z^2}$  [2]

19  $\xi = \{x \text{ is an integer: } 1 \leq x \leq 10\}$

$A = \{\text{factors of } 24\}$

$B = \{\text{prime numbers}\}$

(a) List the elements in

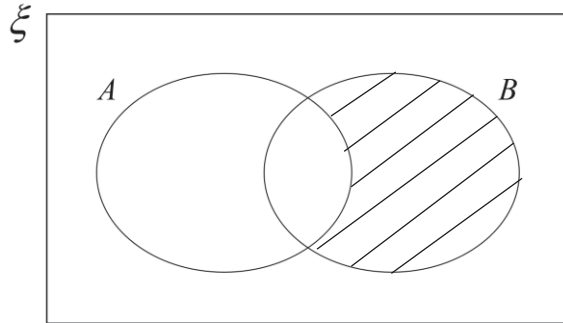
(i)  $A'$ ,

Answer ..... 5, 7, 9, 10 [1]

(ii)  $A \cap B$ .

Answer ..... 2, 3 [1]

(b) On the Venn diagram, shade the region which represents  $(A \cup B)'$ .



[1]

20 (i) Express  $x^2 - 6x + 10$  in the form  $(x - p)^2 + q$ .

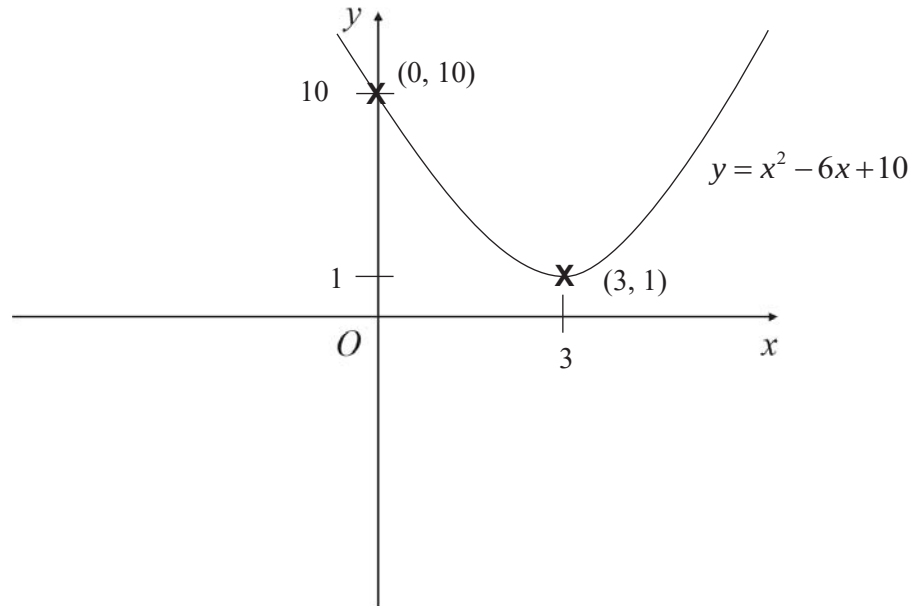
$$\begin{aligned} x^2 - 6x + 10 &= x^2 - 6x + \left(\frac{-6}{2}\right)^2 - \left(\frac{-6}{2}\right)^2 + 10 \\ &= (x - 3)^2 - (-3)^2 + 10 \\ &= (x - 3)^2 + 1 \end{aligned}$$

Answer .....  $(x - 3)^2 + 1$  [2]

(ii) Write down the coordinates of the minimum point of the graph of  $y = x^2 - 6x + 10$ .

Answer (.... 3 ....., ..... 1 .....) [1]

- (iii) Sketch the graph of  $y = x^2 - 6x + 10$  on the axes below.  
Indicate clearly the value where the graph crosses the y-axis.



[2]

- (iv) Explain why the equation  $x^2 - 6x + 10 = k$  does not have solutions for some values of  $k$ .

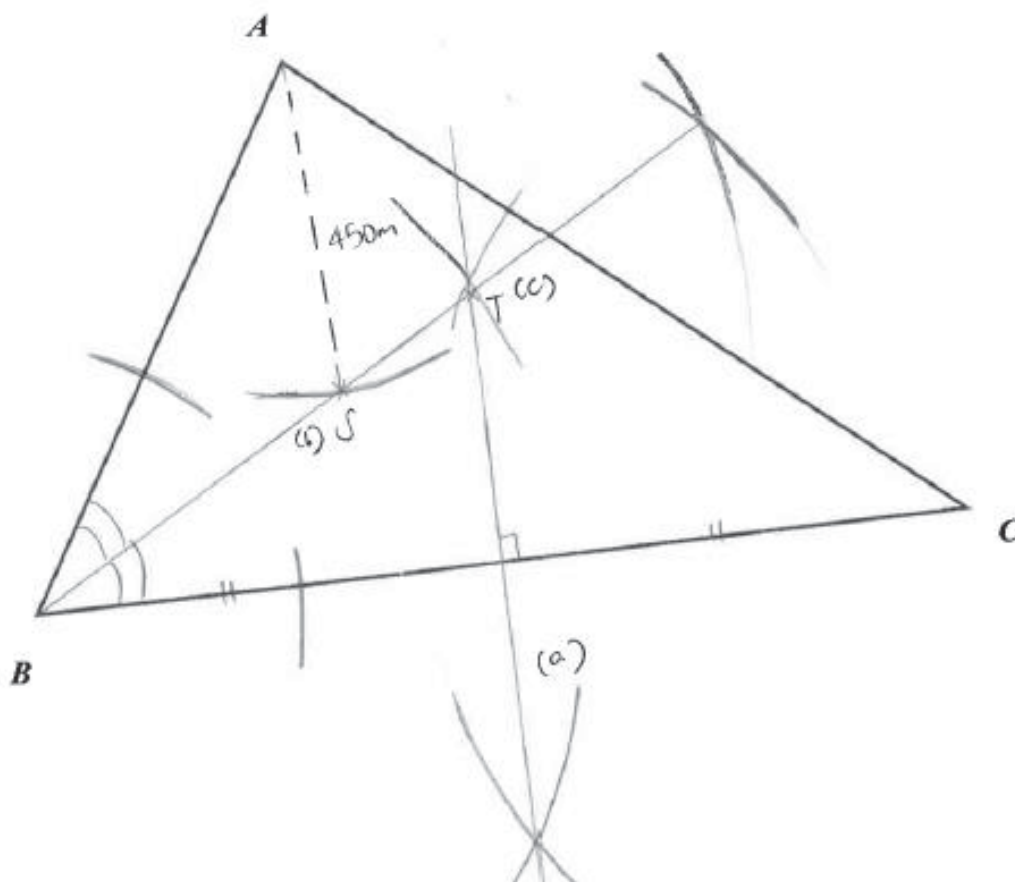
*Answer*

Since the graph will not intersect the line  $y = k$  when  $k < 1$ , there are no solutions when  $k < 1$ .

OR

As  $x^2 - 6x + 10$  will not go below its minimum value of 1, it will not have solutions for  $k < 1$ . [1]

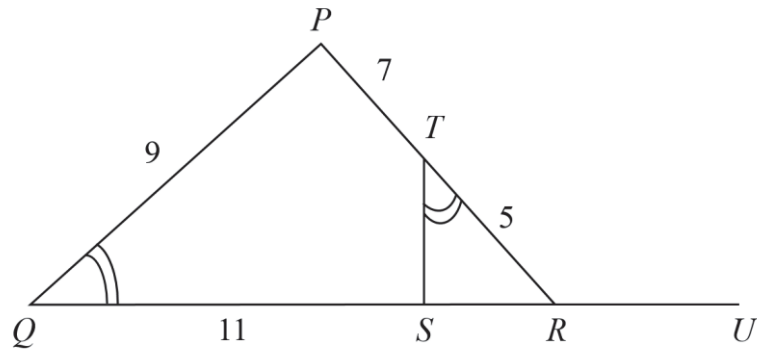
- 21 The diagram is a plan of a triangular field  $ABC$ , drawn to a scale of 1 cm to 100 m.



- (a) Draw the perpendicular bisector of  $BC$ . [1]
- (b) A structure,  $S$ , in the field is 450 m from  $A$  and is equidistant from  $BA$  and  $BC$ . By making appropriate constructions on the diagram, indicate clearly the position of  $S$ . [2]
- (c) Another structure,  $T$ , is to be built equidistant from  $B$  and  $C$  and from  $BA$  and  $BC$ . By locating  $T$ , find the actual distance, in metres from  $S$  to  $T$ .
- Distance =  $2.2 \times 100$   
 = 220 m

Answer ..... 220 ..... m [1]

- 22 In the diagram,  $QSRU$  is a straight line.  $PQ = 9$  cm,  $PT = 7$  cm,  $TR = 5$  cm and  $QS = 11$  cm. Angle  $PQR =$  Angle  $STR$ .



- (a) Show that triangles  $PQR$  and  $STR$  are similar.

*Answer*

$$\angle PQR = \angle STR \text{ (given)}$$

$$\angle PRQ = \angle SRT \text{ (common angle)}$$

Hence triangles  $PQR$  and  $STR$  are similar.

[2]

- (b) Find

- (i) the length of  $SR$ ,

$$\frac{PR}{SR} = \frac{PQ}{ST} = \frac{QR}{TR} \text{ (ratio of corresponding sides are equal)}$$

$$\frac{12}{SR} = \frac{9}{ST} = \frac{11 + SR}{5}$$

$$60 = 11SR + SR^2$$

$$SR^2 + 11SR - 60 = 0$$

$$(SR - 4)(SR + 15) = 0$$

$$SR = 4 \text{ or } SR = -15 \text{ (reject, } SR > 0)$$

$$\text{Answer } SR = \dots\dots\dots 4 \text{ cm [3]}$$

- (ii)  $\cos \angle PRU$ , given that angle  $TSR$  is a right angle.

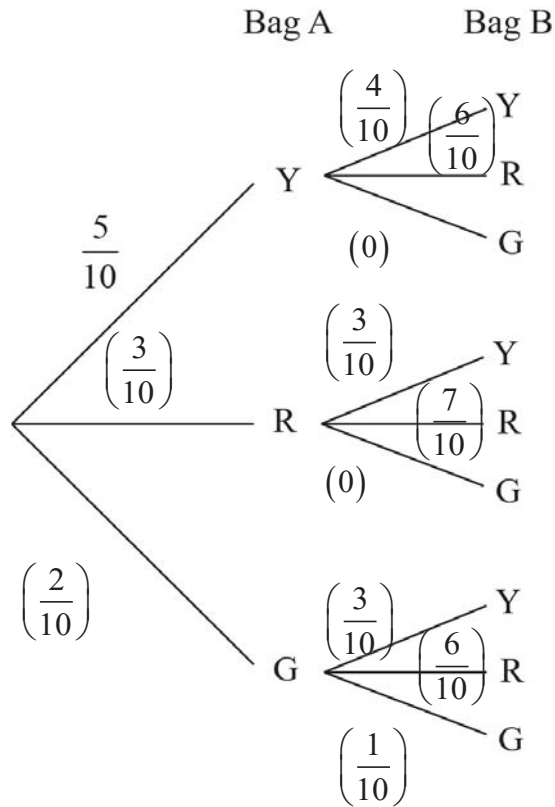
$$\cos \angle PRU = -\cos \angle TRS$$

$$= -\frac{4}{5}$$

$$\text{Answer } \dots\dots\dots -\frac{4}{5} \text{ [1]}$$

- 23 Bag A contains 10 coloured balls of which 5 are yellow, 3 are red and the remaining balls are green. Bag B contains 3 yellow balls and 6 red balls. A ball is drawn at random from Bag A and placed in Bag B. A second ball is then drawn from Bag B.

(i) Complete the tree diagram to show this information.



[2]

(ii) Find the probability that

(a) both balls drawn are of the same colour,

$$P(\text{same colour}) = \left(\frac{5}{10} \times \frac{4}{10}\right) + \left(\frac{3}{10} \times \frac{7}{10}\right) + \left(\frac{2}{10} \times \frac{1}{10}\right)$$

$$= \frac{43}{100}$$

Answer  $\frac{43}{100}$  [2]

(b) both balls drawn are of different colours,

Answer  $\frac{57}{100}$  [1]

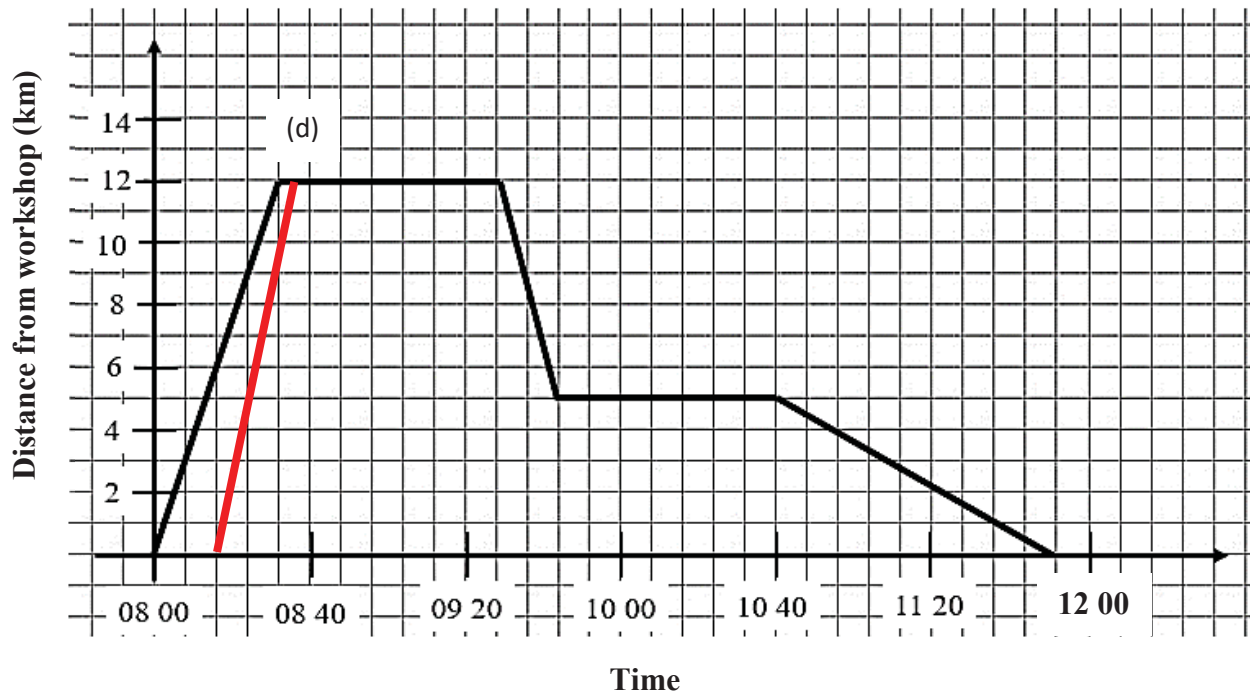
(c) a yellow ball is drawn from Bag B.

$$P(\text{YY, RY, GY}) = \left(\frac{5}{10} \times \frac{4}{10}\right) + \left(\frac{3}{10} \times \frac{3}{10}\right) + \left(\frac{2}{10} \times \frac{3}{10}\right)$$

$$= \frac{7}{20}$$

Answer  $\frac{7}{20}$  [2]

- 24 David drove from his workshop to repair customer A's computer. On his way back, he stopped to repair customer B's computer. The graph shows his entire journey.



- (a) How long did he take to repair both computers in total?

Answer ..... 112 ..... minutes [1]

- (b) How far was he from customer A at 08:24?

Answer ..... 3 or 3.5 ..... km [1]

- (c) Find the speed of his travel from Customer A to Customer B.

$$\begin{aligned} \text{Speed} &= \frac{12}{16/60} \\ &= 26\frac{1}{4} \text{ km/h} \end{aligned}$$

Answer .....  $26\frac{1}{4}$  ..... km/h [1]

- (d) David realised he had forgotten one of his repair tools. His sister, Sarah, left his workshop at 08:16 to bring him his tool. She drove towards customer A's place at a constant speed of 36 km/h. Show her journey on the above graph.

$$\begin{aligned} \text{Time taken} &= \frac{12}{36} \text{ h} \\ &= 20 \text{ min} \rightarrow 2.5 \text{ squares after 08:16} \end{aligned}$$

[1]

## Mathematics Paper 2 Solutions (Prelim 2020)

1 A is the point  $(-20, -11)$  and B is the point  $(8, 10)$ .

(a) Find the equation of the line AB.

$$\begin{aligned}\text{gradient } AB &= \frac{10 - (-11)}{8 - (-20)} \\ &= \frac{3}{4}\end{aligned}$$

Equation of AB:

$$y - 10 = \frac{3}{4}(x - 8)$$

$$y = \frac{3}{4}x - 6 + 10$$

$$y = \frac{3}{4}x + 4$$

$$y = \frac{3}{4}x + 4$$

Answer ..... [2]

(b) Show that the line AB does not pass through the point  $(1, 5)$ .

Answer substitute  $x = 1$  into  $y = \frac{3}{4}x + 4$ ,

$$y = 4\frac{3}{4} \neq 5$$

Since  $(1, 5)$  does not satisfy the equation of AB, AB does not pass through  $(1, 5)$ . [2]

(c) A line  $l$ , perpendicular to the line AB, passes through the point  $(-15, 10)$ .

The product (gradient of  $l$ )  $\times$  (gradient of AB) equals  $-1$ .

Use this information to find the equation of the line  $l$ .

$$m_l \times \frac{3}{4} = -1$$

$$m_l = -\frac{4}{3}$$

Equation of  $l$ :

$$y - 10 = -\frac{4}{3}(x + 15)$$

$$y = -\frac{4}{3}x - 10$$

$$y = -\frac{4}{3}x - 10$$

Answer ..... [2]

(d) The equation of another line  $h$  is  $4x + 3y - 15 = 0$ .

Without solving for  $x$  and  $y$ , explain whether line  $l$  intersects line  $h$ .

Answer

For  $4x + 3y - 15 = 0$

$$y = -\frac{4}{3}x + 5$$

Since gradient of line  $h$  = gradient of line  $l$ , the 2 lines are parallel and hence do not intersect.

[2]

- 2 (a) Each term in this sequence is found by adding the same number to the previous term.

$$a, 1, b, c, 13, \dots$$

- (i) Find the values of  $a$ ,  $b$  and  $c$ .

let the number added be  $x$

$$13 - 3x = 1$$

$$3x = 12$$

$$x = 4$$

$$\therefore a = -3, b = 5, c = 9$$

$$\text{Answer } a = \dots -3 \dots, b = \dots 5 \dots, c = \dots 9 \quad [2]$$

- (ii) Write down, in terms of  $n$ , a formula for the  $n^{\text{th}}$  term.

$$4n - 7$$

$$\text{Answer } \dots\dots\dots 4n - 7 \quad [1]$$

- (ii) Explain why the terms of the sequence are all odd numbers.

*Answer* (1)  $4n$  is an even number and 7 is odd. An even number subtract an odd number will always result in an odd number.

(2)  $4n - 7 = 2\left(2n - \frac{7}{2}\right)$ . As  $\left(2n - \frac{7}{2}\right)$  is not a positive integer,  $4n - 7$  cannot be expressed as a multiple of 2, it is an odd number. [1]

- (b) Observe the following difference of unit fractions.  
(Unit fractions : fractions with numerator equal to 1)

$$\begin{array}{ll} 1^{\text{st}} \text{ line :} & 1 - \frac{1}{2} = \frac{1}{2} \\ 2^{\text{nd}} \text{ line :} & \frac{1}{2} - \frac{1}{3} = \frac{1}{6} \\ 3^{\text{rd}} \text{ line :} & \frac{1}{3} - \frac{1}{4} = \frac{1}{12} \\ & \vdots \\ 10^{\text{th}} \text{ line :} & \frac{1}{10} - \frac{1}{11} = \frac{1}{110} \\ & \vdots \end{array}$$

- (i) Write down the 4<sup>th</sup> line and the 5<sup>th</sup> line.

$$\text{Answer } 4^{\text{th}} \text{ line : } \frac{1}{4} - \frac{1}{5} = \frac{1}{20}$$

$$5^{\text{th}} \text{ line : } \frac{1}{5} - \frac{1}{6} = \frac{1}{30}$$

[2]

- (ii) Write down the  $n^{\text{th}}$  line.

*Answer*       $n^{\text{th}} \text{ line} : \frac{1}{n} - \frac{1}{n+1} = \frac{1}{n(n+1)}$

[1]

- (iii) A student claims that  $\frac{1}{421}$  exists in row  $n$ .

Is he correct? Justify your answers with working.

*Answer*

$$n(n+1) = 421$$

$$n^2 + n - 421 = 0$$

$$n = \frac{-1 \pm \sqrt{(-1)^2 - 4(1)(-421)}}{2}$$

$$n = 20.02.. \quad \text{or} \quad n = -21.0..$$

Since  $n$  is not a positive integer, the student is not correct.

[2]

- (iv) By adding the first 3 lines, we obtain  $1 - \frac{1}{4} = \frac{1}{2} + \frac{1}{6} + \frac{1}{12}$ . Thus,  $1 = \frac{1}{2} + \frac{1}{4} + \frac{1}{6} + \frac{1}{12}$ .

Using this information, express 1 as a sum of seven different unit fractions.

*Answer*

Adding 1<sup>st</sup> 6 lines,

$$1 - \frac{1}{2} + \frac{1}{2} - \frac{1}{3} + \frac{1}{3} - \frac{1}{4} + \frac{1}{4} - \frac{1}{5} + \frac{1}{5} - \frac{1}{6} + \frac{1}{6} - \frac{1}{7} = \frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \frac{1}{42}$$

$$1 - \frac{1}{7} = \frac{1}{2} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \frac{1}{42}$$

$$1 = \frac{1}{2} + \frac{1}{6} + \frac{1}{7} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \frac{1}{42}$$

[1]

- 3 As part of a Values in Action project, three Secondary 4 classes from Brightgrove Secondary School collected old newspapers and clothes to raise funds for charity. The collection was done over two weeks.

The following table shows the weight of the collections made in kilograms (kg), by the three classes, 4E, 4F and 4G in Week 1.

|                 | Week 1 |     |     |
|-----------------|--------|-----|-----|
|                 | 4E     | 4F  | 4G  |
| Newspapers (kg) | 390    | 300 | 350 |
| Clothes (kg)    | 150    | 200 | 180 |

- (a) Represent the weights of the newspapers and clothes collected in Week 1 in a  $2 \times 3$  matrix **A**.

$$\text{Answer } \mathbf{A} = \begin{pmatrix} 390 & 300 & 350 \\ 150 & 200 & 180 \end{pmatrix} \quad [1]$$

- (b) 1 kg of newspapers is sold at \$0.15 and 1 kg of clothes is sold at \$0.45. Represent this information in a  $1 \times 2$  row matrix **H**.

$$\text{Answer } \mathbf{H} = (0.15 \quad 0.45) \quad [1]$$

- (c) The collection done by the same classes in Week 2 is given by the matrix **B**.

$$\mathbf{B} = \begin{pmatrix} 220 & 250 & 200 \\ 260 & 230 & 170 \end{pmatrix}$$

- (i) Evaluate the matrix  $\mathbf{R} = \mathbf{A} + \mathbf{B}$ .

$$\begin{aligned} \mathbf{R} &= \begin{pmatrix} 390 & 300 & 350 \\ 150 & 200 & 180 \end{pmatrix} + \begin{pmatrix} 220 & 250 & 200 \\ 260 & 230 & 170 \end{pmatrix} \\ &= \begin{pmatrix} 610 & 550 & 550 \\ 410 & 430 & 350 \end{pmatrix} \end{aligned}$$

Answer .....  $\begin{pmatrix} 610 & 550 & 550 \\ 410 & 430 & 350 \end{pmatrix}$  [1]

- (ii) Given that  $\mathbf{L} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$ , evaluate the matrix  $\mathbf{M} = \mathbf{RL}$ .

$$\begin{aligned} \mathbf{M} &= \begin{pmatrix} 610 & 550 & 550 \\ 410 & 430 & 350 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \\ &= \begin{pmatrix} 1710 \\ 1190 \end{pmatrix} \end{aligned}$$

Answer .....  $\begin{pmatrix} 1710 \\ 1190 \end{pmatrix}$  [2]

- (iii) State what the elements of **M** represent.

Answer

The elements represent the **total weight of** newspapers and clothes collected **respectively** by the 3 classes, from the **2 collections / weeks**.

[1]

- (iv) Evaluate the matrix **HM**. Hence, state the total amount of money raised by the 3 classes.

$$\begin{aligned} &(0.15 \quad 0.45) \begin{pmatrix} 1710 \\ 1190 \end{pmatrix} \\ &= (256.5 + 535.5) \\ &= (792) \end{aligned}$$

Hence, amount of money raised = \$ 792

Answer \$ .....792..... [2]

- 4 A shop owner bought some essential oil for \$500.  
She paid \$x for each litre of essential oil.

(a) Find, in terms of x, an expression for the number of litres she bought.

$$\frac{500}{x}$$

$$\text{Answer } \dots\dots\dots \frac{500}{x} \quad [1]$$

- (b) Due to a leak, she lost 3 litres of essential oil.  
She sold the remainder of the essential oil for \$1 per litre more than she paid for it.

Write down an expression, in terms of x, for the sum of money she received.

$$\text{no. of litres left} = \frac{500}{x} - 3$$

$$\text{sum of money received} = (x+1)\left(\frac{500}{x} - 3\right)$$

$$\text{Answer } \$ \dots\dots\dots (x+1)\left(\frac{500}{x} - 3\right) \quad [2]$$

- (c) She made a profit of \$20.

Write down an equation to represent this information and show that it reduces to

$$3x^2 + 23x - 500 = 0 .$$

*Answer*

$$(x+1)\left(\frac{500}{x} - 3\right) - 500 = 20$$

$$(x+1)\left(\frac{500}{x} - 3\right) = 520$$

$$500 - 3x + \frac{500}{x} - 3 = 520$$

$$-3x - 23 + \frac{500}{x} = 0$$

$$\times - x] \quad 3x^2 + 23x - 500 = 0 \text{ (shown)}$$

- (d) Solve the equation  $3x^2 + 23x - 500 = 0$ , giving your solutions correct to 2 decimal places.

*Answer*

$$\begin{aligned}
 x &= \frac{-23 \pm \sqrt{(23)^2 - 4(3)(-500)}}{2(3)} \\
 &= \frac{-23 \pm \sqrt{6529}}{6} \\
 x &= 9.633... \quad \text{or} \quad x = -17.300... \\
 &= 9.63(2 \text{ dec.pl}) \quad = -17.30(2 \text{ dec.pl})
 \end{aligned}$$

*Answer*  $x = \dots\dots 9.63\dots\dots$  or  $x = \dots\dots -17.30\dots\dots$  [4]

- (e) Find, correct to the nearest whole number, how many litres of essential oil she sold.

$$\begin{aligned}
 \text{no. of litres sold} &= \frac{500}{9.633...} - 3 \\
 &= 48.90.. \\
 &= 49 \text{ (nearest whole number)}
 \end{aligned}$$

*Answer*  $\dots\dots\dots 49\dots\dots$  [2]

- 5 When  $x$  number of books are printed by a book store, the printing cost, \$ $y$ , of each book can be modelled by the equation

$$y = \frac{240}{x} + 12$$

The table below gives some values of  $x$  and the corresponding values of  $y$ .

|     |    |    |    |    |    |     |     |
|-----|----|----|----|----|----|-----|-----|
| $x$ | 10 | 20 | 30 | 40 | 60 | 80  | 120 |
| $y$ | 36 | 24 | 20 | 18 | 16 | $p$ | 14  |

- (a) Calculate the value of  $p$ .

*Answer*  $p = \dots\dots\dots 15 \dots\dots\dots$  [1]

- (b) On the grid opposite,

use a scale of 2 cm to represent 20 units, draw a horizontal  $x$ -axis for  $0 \leq x \leq 120$ ,  
use a scale of 2 cm to represent 5 units, draw a vertical  $y$ -axis for  $0 \leq y \leq 40$ .

On your axes, plot the points given in the table and join them with a smooth curve. [3]

- (c) Use your graph to estimate the number of books to be printed if the book store wishes to achieve the printing cost of \$19 for each book.

*Answer*  $\dots\dots\dots 34 \dots\dots\dots$  [1]

- (d) By drawing a tangent, find the gradient of the curve at (40, 18).

$$\text{Gradient} = -\frac{24-15}{60-0} = -0.15$$

[actual gradient by differentiation =  $-0.15$ ]

*Answer*  $\dots\dots\dots -0.15 \dots\dots\dots$  [2]

- (e) The selling price of each book is given to be  $\$ \left( 30 - \frac{x}{5} \right)$ .

- (i) On the same grid used in part (b), draw the graph of  $y = \left( 30 - \frac{x}{5} \right)$   
for  $0 \leq x \leq 120$ . [2]

- (ii) Assuming that all printed books are sold, write down a possible value of  $x$  such that the book store will make a profit

[1]

*Answer* Any integer value of  
 $17 \leq x \leq 73$   
 $\dots\dots\dots$



6

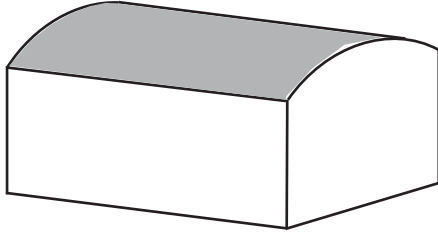


Diagram 1

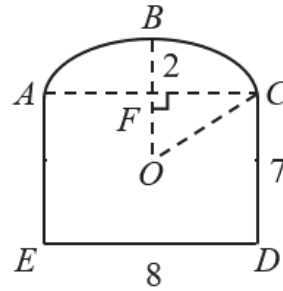


Diagram 2

Diagram 1 shows a garage and Diagram 2 shows the cross section of its end.

The owner needs to order a new roof, represented by the shaded area, for his garage.

The roof is represented by arc  $ABC$ , of a circle with centre  $O$  and radius  $r$  m.  $ACDE$  is a rectangle.  $AC$  intersects  $OB$  at  $F$  and  $\angle OFC = 90^\circ$ .

The owner has these measurements :  $ED = 8$  m ,  $BF = 2$  m ,  $CD = 7$  m , and the length of the garage is 12 m.

- (a) By expressing  $OF$  in terms of  $r$ , show that  $r = 5$  m .

*Answer*

$$OF = r - 2$$

$$OC^2 = OF^2 + FC^2$$

$$r^2 = (r - 2)^2 + 4^2$$

$$r^2 = r^2 - 4r + 4 + 16$$

$$4r = 20$$

$$r = 5 \text{ (shown)}$$

[3]

- (b) Show that angle  $AOC$  is approximately 1.855 radians.

*Answer*

Consider triangle  $FOC$ ,

$$\frac{CF}{OC} = \sin \angle FOC$$

$$\sin \angle FOC = \frac{4}{5}$$

$$\angle FOC = \sin^{-1} \left( \frac{4}{5} \right)$$

$$= 0.92729...$$

$$\angle AOC = 2(0.92729...)$$

$$= 1.8545...$$

$$= 1.855 \text{ (4 sig.fig) (shown)}$$

[2]

- (c) The material for the roof costs \$12.50 per  $\text{m}^2$ .

Find the cost of the new roof. Give your answer to the nearest dollar.

$$\begin{aligned}\text{Arc length ABC} &= 5(1.8545\dots) \\ &= 9.2729\dots \\ \text{surface area} &= 9.2729\dots \times 12 \\ &= 111.2754\dots \\ \text{Cost of new roof} &= 111.2754\dots \times \$12.50 \\ &= \$1390.94\dots \\ &= \$1391 \text{ (nearest dollar)}\end{aligned}$$

Answer \$ .....1391..... [3]

- (d) Calculate the volume of the garage.

$$\begin{aligned}\text{Area of sector} &= \frac{1}{2}(5)^2(1.8545\dots) \\ &= 23.1812\dots \\ \text{Area of triangle AOC} &= \frac{1}{2}(5)^2 \sin(1.8545\dots) \\ &= 12.000\dots \\ \text{Area of segment} &= 23.1812\dots - 12.000\dots \\ &= 11.18088\dots \\ \therefore \text{Volume of garage} &= (11.18088\dots + 7(8)) \times 12 \\ &= 806.17\dots \\ &= 806 \text{ m}^3 \text{ (3 sig.fig)}\end{aligned}$$

**Alternative method**

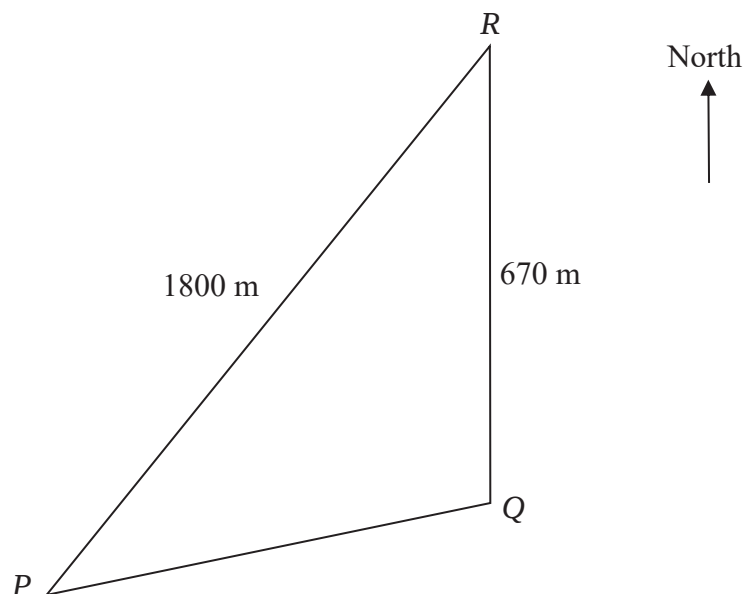
$$\begin{aligned}\text{Area of sector} &= \frac{1}{2}(5)^2(1.8545\dots) \\ &= 23.1812\dots \\ \text{Area of AOCDE (2 trapeziums)} &= 2 \times \frac{1}{2}(4+7)(4) \\ &= 44 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Volume of garage} &= \text{area of cross section} \times 12 \\ &= (23.1812\dots + 44) \times 12 \\ &= 67.1812\dots \times 12 \\ &= 806.1744\dots \\ &= 806 \text{ cm}^3\end{aligned}$$

Answer .....806..... $\text{m}^3$  [4]



7



$P$ ,  $Q$  and  $R$  represent three points on an island.  
 $Q$  is 670 m from  $R$  and  $Q$  is due south of  $R$ .  
 $P$  is 1800 m from  $R$ .

- (a) Given that the bearing of  $P$  from  $R$  is  $235^\circ$ , show that angle  $PRQ = 55^\circ$ .

Answer

$$\begin{aligned}\angle PRQ &= 235^\circ - 180^\circ \\ &= 55^\circ \text{ (shown)}\end{aligned}$$

[1]

- (b) Calculate  $PQ$ .  
 Using Cosine Rule,

$$\begin{aligned}PQ &= \sqrt{(1800)^2 + (670)^2 - 2(1800)(670)\cos 55^\circ} \\ &= 1518.365\dots \\ &= 1520 \text{ m (3 s.f.)}\end{aligned}$$

Answer .....1520..... [2]

- (c) Find the bearing of  $Q$  from  $P$ .

$$\frac{\sin \angle QPR}{670} = \frac{\sin 55^\circ}{PQ} \quad [\text{Sine Rule}]$$

$$\sin \angle QPR = \frac{670 \times \sin 55^\circ}{(1518.365\dots)}$$

$$\angle QPR = 21.1900\dots^\circ$$

$$\angle N_1PQ = 21.1900\dots^\circ + 55^\circ$$

$$= 76.19\dots^\circ$$

$$\therefore \text{Bearing of } Q \text{ from } P = 076.2^\circ \text{ (1d.p)}$$

|                                 |
|---------------------------------|
| Will be 21.166<br>(if use 1520) |
|---------------------------------|

Answer .....076.2°..... [3]

- (d) A hiker walks in a straight line from  $P$  to  $R$  and stops at a rest point  $X$ , where  $X$  is closest to  $Q$ . Calculate  $PX$ .

$$QX \perp PR$$

$$\cos 55^\circ = \frac{XR}{670}$$

$$XR = 670 \cos 55^\circ$$

$$\text{OR } \cos 21.1900^\circ = \frac{PX}{1518.365...}$$

$$PX = 1420 \text{ m (3sf)}$$

$$\therefore PX$$

$$= 1800 - 670 \cos 55^\circ$$

$$= 1415.703 \text{ m}$$

$$= 1420 \text{ m (3sf)}$$

Answer ..... 1420 ..... m [2]

- (e) At  $X$ , the hiker spots an eagle hovering vertically above  $R$ .  
The angle of elevation of the eagle from  $X$  is  $23.1^\circ$ .

Calculate the height of the eagle from the ground.

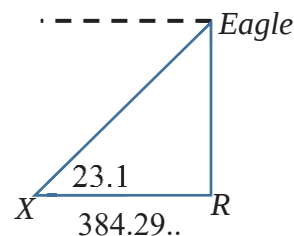
$$\tan 23.1^\circ = \frac{\text{Height of eagle}}{1800 - 1415.703...}$$

Height of eagle

$$\tan 23.1^\circ \times 384.297..$$

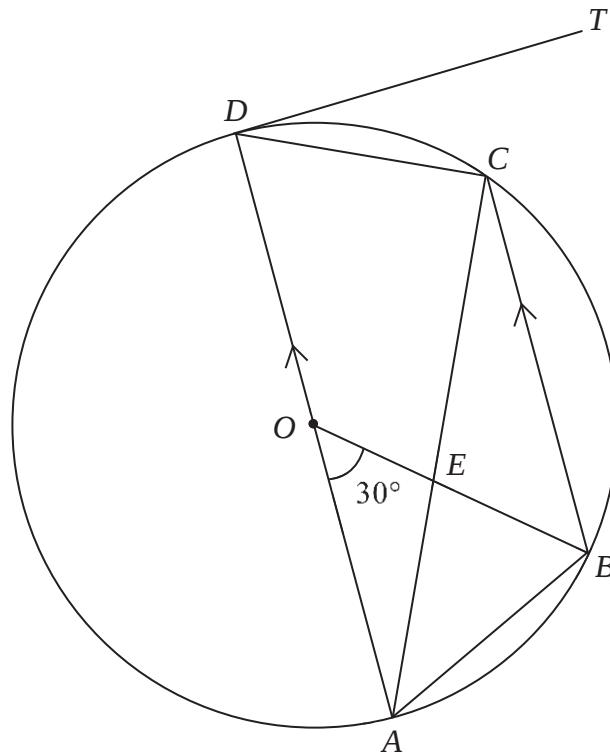
$$= 163.9165...$$

$$= 164 \text{ m (3 sig.fig)}$$



Answer ..... 164 ..... m [2]

- 8 In the diagram,  $A, B, C$  and  $D$  are points on the circumference of a circle with centre  $O$ .  $TD$  is a tangent to the circle.  $AD$  is a diameter of the circle and  $TD$  is a tangent to the circle.  $OB$  intersect  $AC$  at  $E$ , angle  $AOB = 30^\circ$  and  $AD$  is parallel to  $BC$ .



(a) Find, giving reasons to your workings,

(i) angle  $BCA$ ,

$$\begin{aligned}\angle BCA &= 30^\circ \div 2 \quad (\angle \text{ at centre} = 2\angle \text{ s at circumference}) \\ &= 15^\circ\end{aligned}$$

Answer .....  $15^\circ$  ..... [1]

(ii) angle  $CDA$ ,

$$\angle ACD = 90 \quad (\text{right angle in semicircle})$$

$$\angle CAO = \angle BCA = 15^\circ \quad (\text{alternate angles, } BC \parallel AD)$$

$$\begin{aligned}\therefore \angle CDA &= 180^\circ - 15^\circ - 90^\circ \quad (\angle \text{ sum of triangle}) \\ &= 75^\circ\end{aligned}$$

Answer .....  $75^\circ$  ..... [2]

(iii) angle  $ABC$ ,

$$\begin{aligned}\angle ABC &= 180^\circ - \angle CDA \text{ (}\angle\text{s in opposite segment)} \\ &= 180^\circ - 75^\circ \\ &= 105^\circ\end{aligned}$$

Answer .....  $105^\circ$  [2]

(iv) angle  $TDC$ .

$$\begin{aligned}\angle ODT &= 90^\circ \text{ (tangent } \perp \text{ radius)} \\ \angle TDC &= 90^\circ - 75^\circ \\ &= 15^\circ\end{aligned}$$

Answer .....  $15^\circ$  [2]

(b) It is given that angle  $BXA =$  angle  $BCA$ .

Explain whether point  $X$  should lie inside, on or outside the circle.

Answer

Since  $\angle BXA = \angle BCA$ , the two angles must be in the **same segment**.

Hence  $X$  should lie **on** the circle.

OR

$X$  should lie outside the circle, such that

$BC = BX$  and  $CAX$  lie on a straight line

(or triangle  $BCX$  is isosceles).

[2]

(c) “A circle with diameter  $AC$  can be drawn through the points  $A$ ,  $B$  and  $C$ .”

Determine, with clear explanation, if the above statement is true or false.

Answer

$$\angle ABC = 105^\circ \neq 90^\circ$$

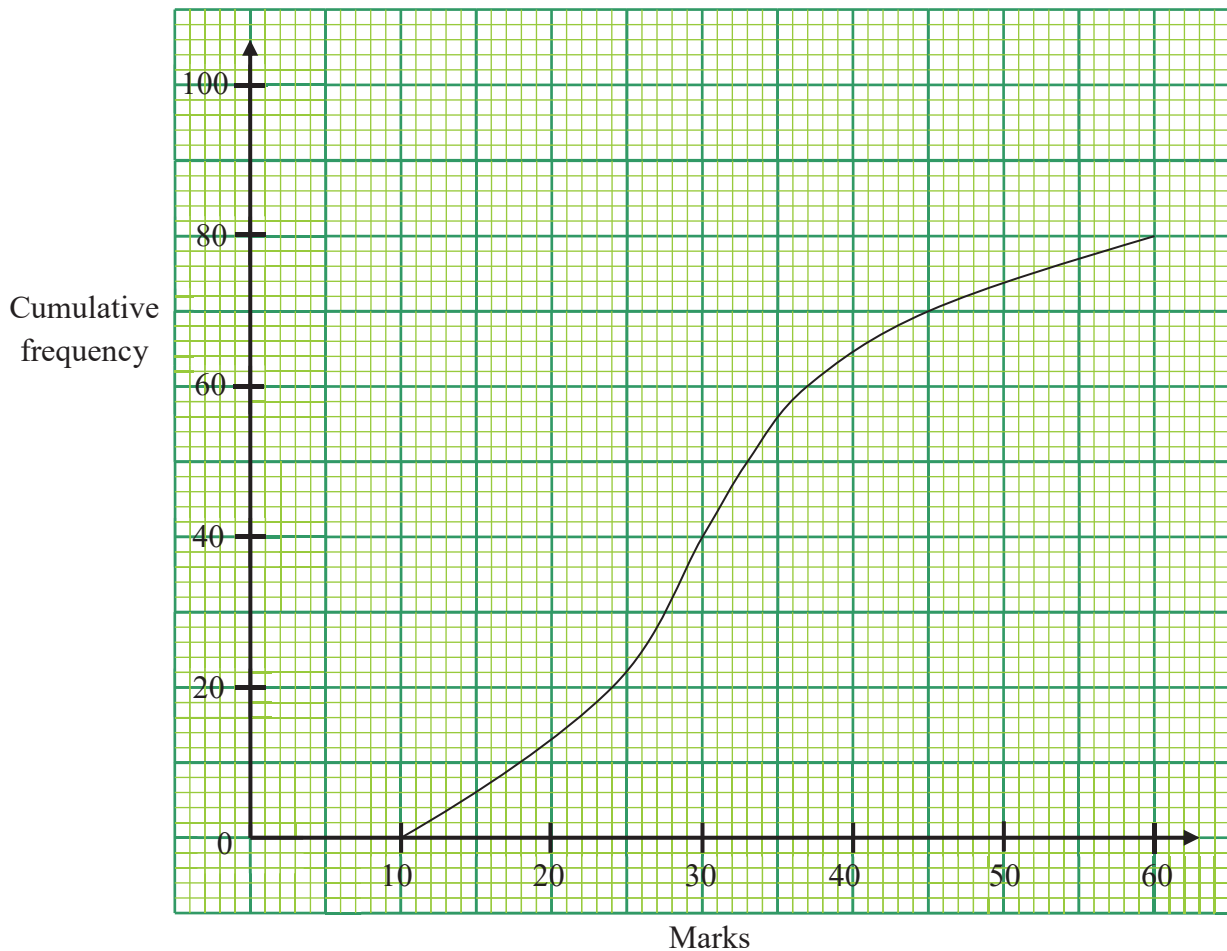
Since angle property right angle in a semicircle is not fulfilled,

$AC$  cannot be the diameter of the circle.

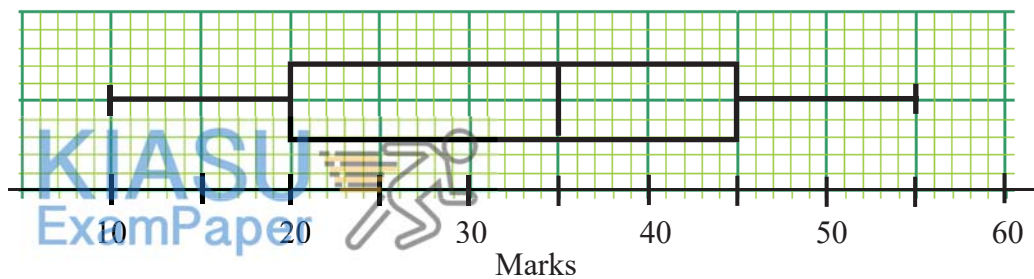
The statement is false.

[2]

- 9 (a) The cumulative frequency graph shows the distribution of the scores of a Geography test (Test 1) taken by 80 students. Test 1 was marked out of 60.



This box-and-whisker plot represents the distribution of the scores of the same group of students for another Geography Test (Test 2). Test 2 was marked out of 60.



- (i) Use the two diagrams to complete this table for the two tests.

| Test | Lower Quartile | Median    | Upper Quartile | Interquartile range |
|------|----------------|-----------|----------------|---------------------|
| 1    | <b>24</b>      | 30        | <b>37</b>      | <b>13</b>           |
| 2    | 20             | <b>35</b> | 45             | 25                  |

[3]

To obtain a distinction for Test 1 and Test 2, a student needs to score at least  $x$  marks.

- (ii) If 12.5% of the students scored distinction for Test 1, find  $x$ .

87.5% scored  $< x$  marks

87.5% of 80 = 70 students

$x = 45$

Answer .....45 [2]

- (iii) “There is a higher proportion of students who scored distinction for Test 1.”

Do you agree with this statement? Give a reason for your answer.

Answer

I disagree with the statement.

The upper quartile for Test 2 is 45 marks, which means that 25% of students scored distinction for Test 2, which is more than that of Test 1 (12.5%). A higher proportion of student scored distinction for Test 2 instead of Test 1.

[2]

- (b) The table below summarises the speeds of 95 cars on a stretch of road.

| Speed<br>( $x$ km/h) | $35 < x \leq 45$ | $45 < x \leq 55$ | $55 < x \leq 65$ | $65 < x \leq 75$ | $75 < x \leq 85$ |
|----------------------|------------------|------------------|------------------|------------------|------------------|
| Number<br>of cars    | 13               | 29               | 40               | 8                | 5                |

Calculate an estimate of

- (i) the mean speed,

Answer .....56.1..... km/h

[1]

- (ii) the standard deviation.

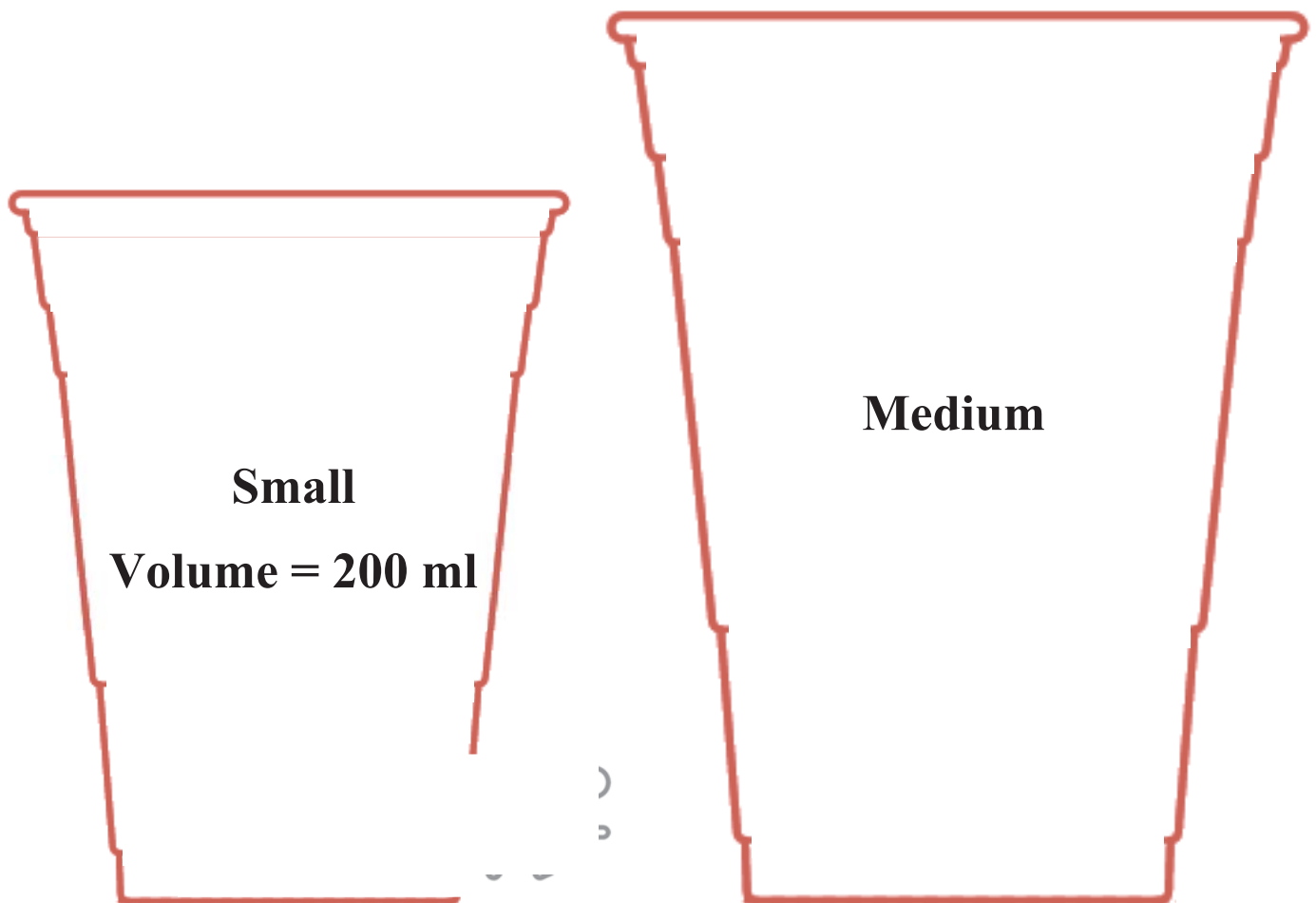
Answer .....9.98 [1]

- 10 DeBest Bubble Tea Shop purchases their plastic cups from Bubble Planet Supplies. Below is a pamphlet on the dimensions of the plastic cups. Due to printing problems, some information are missing.

### **BUBBLE PLANET SUPPLIES**

Picture shows actual size of cup

|                 |                   |
|-----------------|-------------------|
| Item type       | Plastic Cup       |
| Sizes Available | Small, Medium     |
| Uses            | Drinks (Hot/Cold) |



- (a) Estimate the heights of the small and medium cup.

*Answer* Height of small cup : .....<sup>9.9</sup>..... cm

Height of medium cup : .....<sup>12.4</sup>..... cm [1]

- (b) Given that the two cups are geometrically similar, find the volume of the medium cup.

$$\left(\frac{12.4}{9.9}\right)^3 = \frac{V_M}{200}$$

$$V_M = \left(\frac{12.4}{9.9}\right)^3 \times 200$$

$$= 392.99...$$

$$= 393 \text{ ml (3 sig.fig)}$$

*Answer* .....<sup>393</sup>.....ml [2]

- (c) Allison is planning to order a drink from DeBest Bubble Tea Shop. She has read the following health advice:

To avoid developing diabetes, the Health Promotion Board (HPB) recommends a daily calorie intake from sugary food (e.g. a cup of bubble tea) of no more than 10% of one's daily energy intake.

She then finds the following information on the website of DeBest Bubble Tea Shop.

**Table 1**

| <b>Sugar Level</b>  |
|---------------------|
| Quarter Sugar (25%) |
| Half Sugar (50%)    |
| Less Sugar (75%)    |
| Full Sugar (100%) * |

\* A medium-sized cup of drink with full sugar (100%) contains 95 ml of sugar syrup.

**Table 2**

|                    | <b>Approximate amount of calories</b> |
|--------------------|---------------------------------------|
| <b>Green tea</b>   | 85 calories per 500 ml                |
| <b>Milk tea</b>    | 110 calories per 500 ml               |
| <b>Black tea</b>   | 70 calories per 500 ml                |
| <b>Sugar syrup</b> | 50 calories per 15 ml                 |
| <b>Honey</b>       | 60 calories per 15 ml                 |

Note : A cup of flavoured tea is made by adding sugar syrup according to customers' preferred sugar level and topping up the remaining amount with flavoured tea.

**For customers with daily energy intake between 2400 and 2900 calories**

**Healthier Choice Option**

**Medium-sized milk tea with 75% sugar level**

Allison's daily energy intake is about 2800 calories.

She decides to select the healthier choice option drink and thinks that she will meet the daily calorie intake as recommended by HPB.

Is she correct?

Justify your decision with calculations.

**Writing space for Q10 (c)***Answer:*

volume of medium cup = 393 ml

Amount of sugar syrup in 75%

$$= 0.75 \times 95$$

$$= 71.25 \text{ ml}$$

Amount of milk tea

$$= 393 - 71.25$$

$$= 321.75 \text{ ml}$$

Amount of calories in :

$$\begin{aligned} \text{Sugar syrup} &= \frac{71.25}{15} \times 50 \\ &= 237.5 \end{aligned}$$

$$\begin{aligned} \text{milk tea} &= \frac{321.75}{500} \times 110 \\ &= 70.785 \end{aligned}$$

total number of calories from 1 cup of bubble tea

$$= 237.5 + 70.785$$

$$= 308.285$$

$$= 308 \text{ calories (3 sig.fig)}$$

Allison's recommended daily calorie  
intake from sugary food

$$= \frac{10}{100} \times 2800$$

$$= 280$$

since  $308 > 280$ , Allison will not  
meet the recommendation by HPB.

She is not correct.

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