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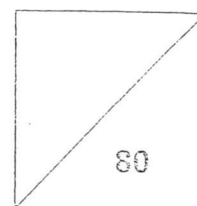
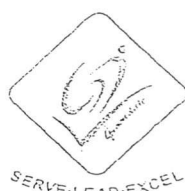
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Name: \_\_\_\_\_ ( )

Class: \_\_\_\_\_



## GREENDALE SECONDARY SCHOOL End-of-Year Examination 2014

### MATHEMATICS

4042/01

Paper 1

10 October 2014

Secondary Three Normal Academic

2 hours

Candidates answer on the Question Paper.

### READ THESE INSTRUCTIONS FIRST

Write your index number and name on all the work you hand in.

Write in dark or blue pen.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working may result in loss of marks.

You are expected to use a scientific calculator to evaluate explicit numerical expressions.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142, unless the question required the answer in terms of  $\pi$ .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 80.

| Question | Q1 | Q2 | Q3 | Q4 | Q5 | Q6 | Q7 | Q8 | Q9 | Q10 | Q11 | Q12 | Q13 |
|----------|----|----|----|----|----|----|----|----|----|-----|-----|-----|-----|
| Strand   | N  | N  | A  | S  | N  | G  | N  | N  | N  | G   | S   | G   | M   |
| Marks    | 2  | 2  | 2  | 2  | 4  | 2  | 2  | 3  | 3  | 4   | 3   | 4   | 4   |

| Question | Q14 | Q15 | Q16 | Q17 | Q18 | Q19 | Q20 | Q21 | Q22 | Q23 | Q24 |  |
|----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--|
| Strand   | N   | A   | A   | N   | G   | S   | G   | M   | A   | M   | A   |  |
| Marks    | 3   | 3   | 4   | 4   | 5   | 3   | 3   | 4   | 5   | 4   | 5   |  |

This document consists of 18 printed pages, including this cover page.

Answer all the questions.

1. (a) Express 25% as a fraction in its lowest terms.

Answer (a) \_\_\_\_\_ [1]

- (b) Express  $\frac{1}{40}$  as a decimal.

Answer (b) \_\_\_\_\_ [1]

2. By writing each number correct to 1 significant figure, estimate the value of

$$\frac{58.4 \times 0.46}{13.2}$$

You need to show your working.

Answer \_\_\_\_\_ [2]

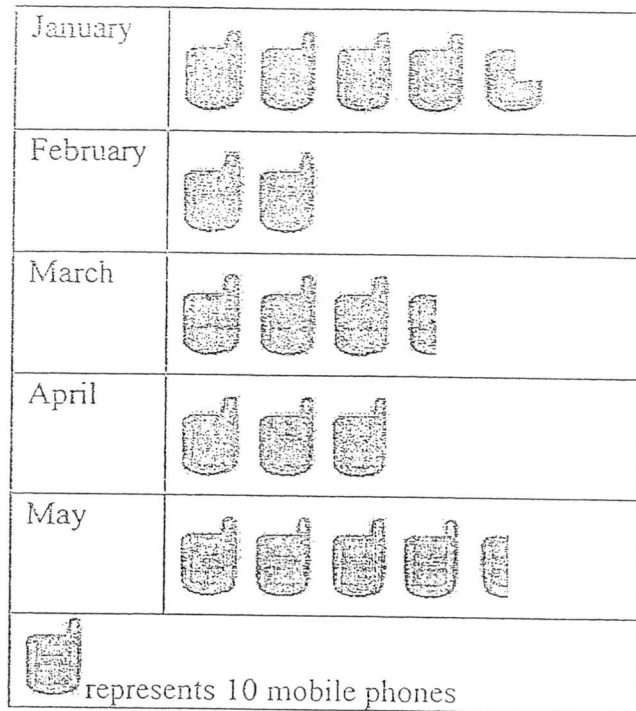
3. Simplify  $\frac{2x+3}{3} - \frac{x}{2}$ .

Answer \_\_\_\_\_ [2]

---

For Examiner's  
Use Only

4. The pictogram below shows the sales of mobile phones of a company from January 2008 to May 2008.



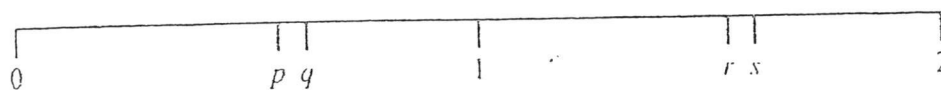
- (a) How many mobile phones were sold in the month of April?

Answer (a) \_\_\_\_\_ mobile phones [1]

- (b) Which month registered the highest sales of mobile phones?

Answer (b) \_\_\_\_\_ [1]

5. The numbers  $p$ ,  $q$ ,  $r$ , and  $s$  are represented on a number line.



The values of  $p$ ,  $q$ ,  $r$  and  $s$  are listed below.

$$\frac{7}{5} \quad 0.75 \quad \frac{3}{5} \quad \frac{\pi}{2}$$

Find  $p$ ,  $q$ ,  $r$  and  $s$ .

Answer (a)  $p =$  \_\_\_\_\_ [1]

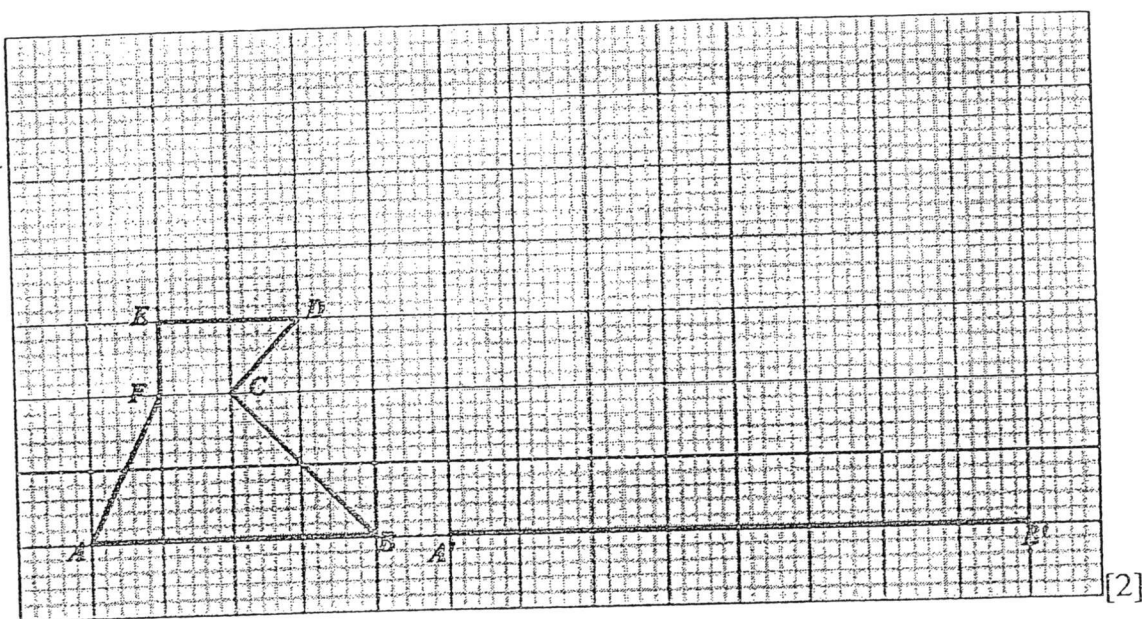
$q =$  \_\_\_\_\_ [1]

$r =$  \_\_\_\_\_ [1]

$s =$  \_\_\_\_\_ [1]

6. Enlarge the given figure in the grid below by a scale factor of 2 and draw the enlarged figure within the grid.

$A'B'$  of the enlarged figure has been drawn for you.



7. In January 2014, the rate of exchange of Singapore dollar to Japanese yen was  $\text{S\$}1 = \text{¥}250$ .

- (a) Ali exchanged  $\text{S\$}850$  to Japanese yen for his business trip.  
How much Japanese yen did he receive?

Answer(a) ¥ \_\_\_\_\_ [1]

- (b) He spent  $\text{¥}24\,600$  in Japan, and exchanged the remaining yen into dollars when the exchange rate was  $\text{\$}1 = \text{¥}260$ .

How much dollars did he receive? Give your answer to the nearest dollar.

Answer (b) S\\$ \_\_\_\_\_ [1]

8. Melvin leaves home at 7:45am, and arrives at work at 9:10am.

- (a) How long did Melvin take to go to work? Leave your answer in hours and minutes.

Answer (a) \_\_\_\_\_ hours \_\_\_\_\_ minutes [1]

- (b) Given that Melvin travelled 15km to work, find his average speed, in kilometres per hour.

Answer (b) \_\_\_\_\_ km/h [2]

---

9. (a) Express the ratio of 8 months to 2 years 4 months as a ratio in its simplest form

Answer (a) \_\_\_\_\_ : \_\_\_\_\_ [1]

- (b) \$40 is divided in the ratio of  $p : q$  where  $p < q$ .  
Write down an expression in terms of  $p$  and  $q$ , for the smaller amount.

Answer (b) \$ \_\_\_\_\_ [2]

10. (a) Show that the sum of interior angles of a 7-sided polygon is  $900^\circ$ .

Answer (a) \_\_\_\_\_  $^\circ$  [1]

- (b) Four of the angles of a 7-sided polygon are  $120^\circ$ , and the others are  $x^\circ$ ,  $(x + 92)^\circ$  and  $(2x - 20)^\circ$ . Find the largest angle.

Answer (b) \_\_\_\_\_  $^\circ$  [3]

---

11. The stem and leaf diagram below shows the waiting times (in minutes) of some patients in a clinic.

| Stem | Leaves    |
|------|-----------|
| 1    | 5 6       |
| 2    | 0 1 3 7 8 |
| 3    | 0 0 2 4 6 |
| 4    | 1 2 4     |
| 5    | 3         |
| 6    | 1         |

Key : 4 | 1 represent 41 minutes

Find

- (a) the maximum waiting time,

Answer (a) \_\_\_\_\_ minutes [1]

- (b) the total number of patients,

Answer (b) \_\_\_\_\_ patients [1]

- (c) the modal waiting time.

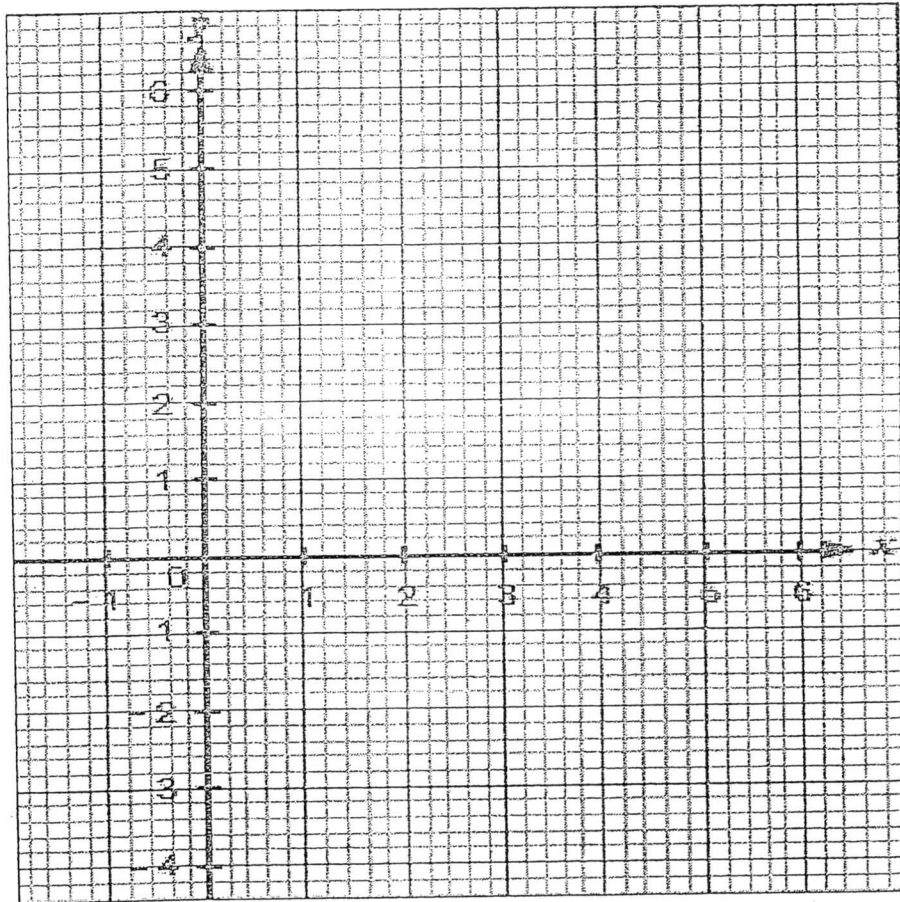
Answer (c) \_\_\_\_\_ minutes [1]

12. (a) Complete the table of values for
- $y = 2x + 1$
- .

|     |    |   |   |
|-----|----|---|---|
| $x$ | -1 | 0 | 2 |
| $y$ |    | 1 |   |

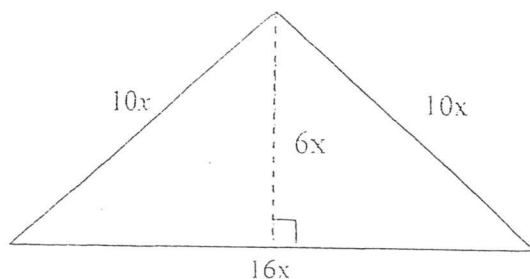
[2]

- (b) On the grid below, draw the graph of
- $y = 2x + 1$
- .



[2]

13. The perimeter of the triangle as shown below is 360 cm.  
It has a base of  $16x$  cm and height of  $6x$  cm.



Find

- (a) the value of  $x$ ,

Answer (a) \_\_\_\_\_ [2]

- (b) the area of the triangle.

Answer (b) \_\_\_\_\_ [2]

14.  $y$  is directly proportional to  $x^2$ .  
Given that  $y = 27$  when  $x = 9$ , find

- (a) an expression for  $y$  in terms of  $x$ ,

Answer (a)  $y =$  \_\_\_\_\_ [2]

- (b) Hence, find the value of  $x$  when  $y = \frac{1}{12}$ .

Answer (b)  $x =$  \_\_\_\_\_ [1]

15. (a) Evaluate  $4^{-2}$ .

Answer (a) \_\_\_\_\_ [1]

- (b) Given that  $27^{\frac{2}{3}} = 3^x$ , find  $x$ .

Answer (b) \_\_\_\_\_ [2]

16. (a) Given that  $x^2 - 4x + 7 = (x - p)^2 + q$ , find  $p$  and  $q$ .

Answer (a)  $p =$  \_\_\_\_\_ [1]

$q =$  \_\_\_\_\_ [1]

- (b) Hence, or otherwise, solve  $x^2 - 4x + 7 = 3$ .

Answer (b) \_\_\_\_\_ [2]

17. The figures below show a sequence of patterns consisting of circles and triangles joined by the lines. The first three patterns are shown below.

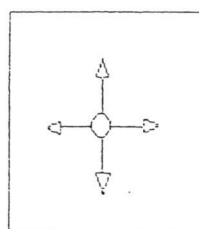


Figure 1

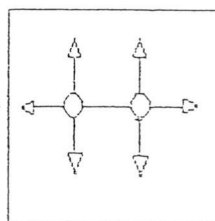


Figure 2

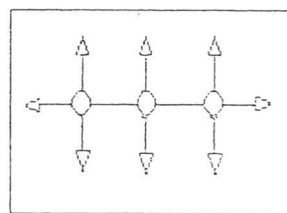


Figure 3

- (a) Draw the next figure in the space provided.

[1]

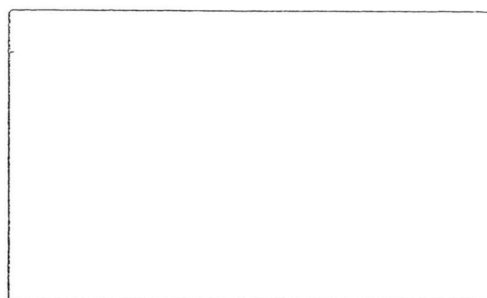


Figure 4

- (b) The table below shows the tabulation of the number of  $\bigcirc$  and  $\triangle$  for each figure.

Complete the table below by filling in the blanks for figures 4.

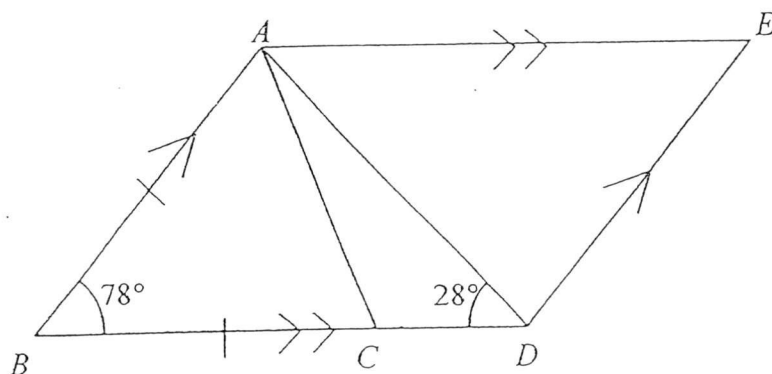
[1]

| Figure | Number of $\bigcirc$ | Number of $\triangle$ |
|--------|----------------------|-----------------------|
| 1      | 1                    | 4                     |
| 2      | 2                    | 6                     |
| 3      | 3                    | 8                     |
| 4      |                      |                       |

- (c) Write down in terms of  $n$ , the number of  $\triangle$  in the  $n^{\text{th}}$  figure.

Answer (c) \_\_\_\_\_ [2]

18. In the figure below,  $ABDE$  is a parallelogram.  
 $AB = BC$ ,  $\angle ABC = 78^\circ$  and  $\angle ADC = 28^\circ$ .



Writing down the reasons clearly, find the value of

- (a)  $\angle AED$ ,

Answer (a)  $\angle AED =$  \_\_\_\_\_<sup>0</sup> [1]

- (b)  $\angle DAE$ ,

Answer (b)  $\angle DAE =$  \_\_\_\_\_<sup>0</sup> [1]

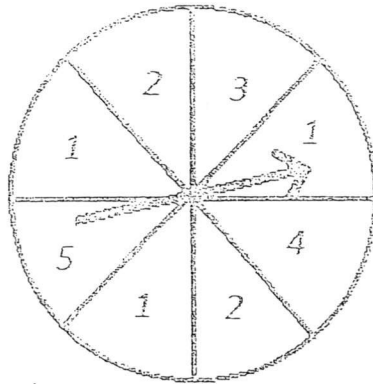
- (c)  $\angle BAE$ ,

Answer (c)  $\angle BAE =$  \_\_\_\_\_<sup>0</sup> [1]

- (d)  $\angle ACD$ ,

Answer (d)  $\angle ACD =$  \_\_\_\_\_<sup>0</sup> [2]

19. The diagram shows a wheel.



Joel spins the wheel once. What is the probability that Joel obtains

- (a) a score of 1,

Answer (a) \_\_\_\_\_ [1]

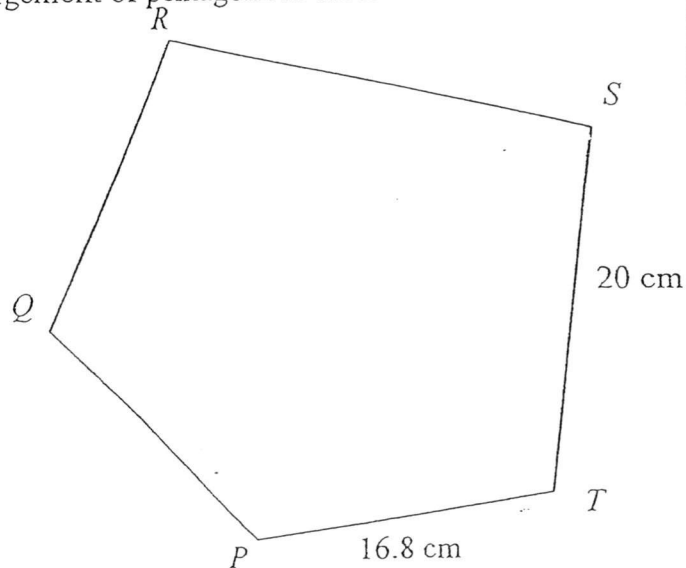
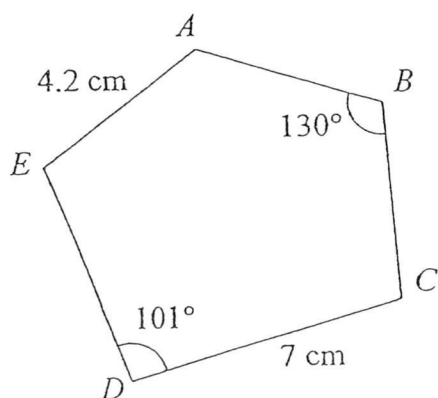
- (b) a score of an even number,

Answer (b) \_\_\_\_\_ [1]

- (c) a score that is not a 2?

Answer (c) \_\_\_\_\_ [1]

20. Pentagon  $PQRST$  is an enlargement of pentagon  $ABCDE$ .



Find

- (a) the scale factor of the enlargement,

Answer (a) \_\_\_\_\_ [1]

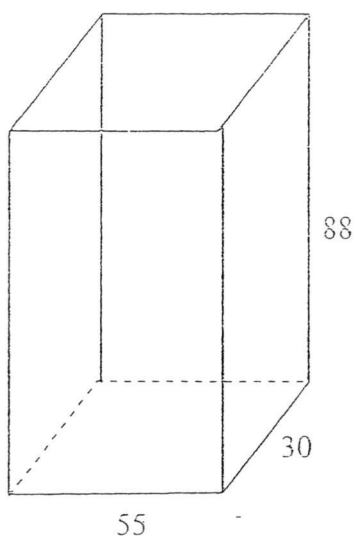
- (b)  $\angle RST$ ,

Answer (b) \_\_\_\_\_  $^\circ$  [1]

- (c)  $RS$ .

Answer (c) \_\_\_\_\_  $\text{cm}$  [1]

21. The diagram below shows a brick in the form of a rectangular cuboid.



(a) Calculate

- (i) the volume of the brick.

Answer (a)(i) \_\_\_\_\_  $\text{cm}^3$  [1]

- (ii) the total surface area of the brick.

Answer(a)(ii) \_\_\_\_\_  $\text{cm}^2$  [2]

- (b) The brick will be painted with a special layer of water-proof material.  
It cost \$0.02 per square centimetre to paint it.

Calculate the cost of painting the brick.

Answer(b) \$ \_\_\_\_\_ [1]

22. (a) Solve  $\frac{1}{4}x - 3 = 1$

Answer (a)  $x =$  \_\_\_\_\_ [1]

(b) Solve  $3(x - 2)(x + 4) = 0$

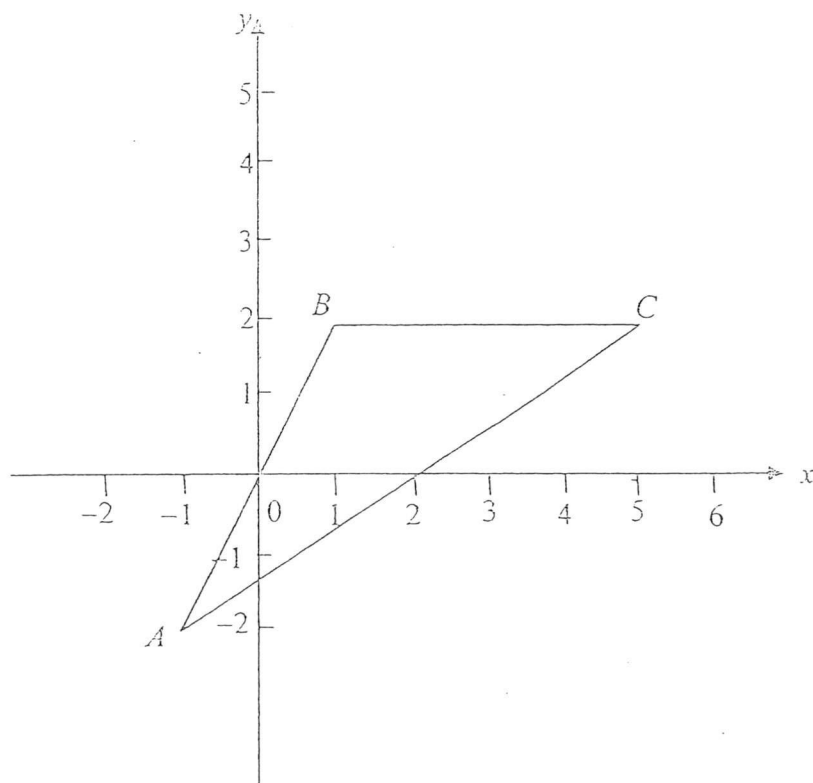
Answer (b)  $x =$  \_\_\_\_\_ or  $x =$  \_\_\_\_\_ [2]

(c) Solve  $3y^2 - 5y - 4 = 0$ , giving each answer correct to 2 decimal places.

(b)  $y =$  \_\_\_\_\_ or  $y =$  \_\_\_\_\_ [2]

---

23. The points  $A(1, 2)$ ,  $B(5, 2)$ ,  $C(-1, -2)$  and  $D$  are vertices of parallelogram  $ABCD$ .



Find

- (a) the gradient of  $BC$ ,

Answer (a) \_\_\_\_\_ [1]

- (b) the length of  $AC$ ,

Answer (b) \_\_\_\_\_ units [1]

- (c) the area of triangle  $ABC$ .

Answer (c) \_\_\_\_\_  $\text{cm}^2$  [1]

- (d) State the co-ordinates of  $D$ .

Answer (d) ( \_\_\_\_\_ , \_\_\_\_\_ ) [1]

24. Given that

$$\bigcirc \bigcirc \star \star \star = 78$$

$$\bigcirc \star = 30$$

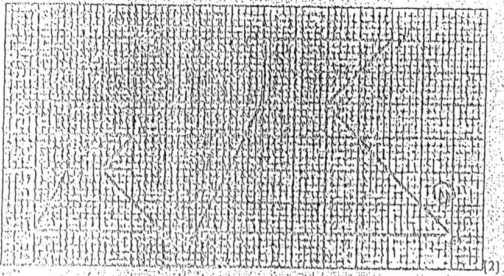
- (a) Let  $x$  be  $\bigcirc$  and  $y$  be  $\star$ , write down two simultaneous equations in  $x$  and  $y$ .

Answer (a) \_\_\_\_\_  
\_\_\_\_\_ [2]

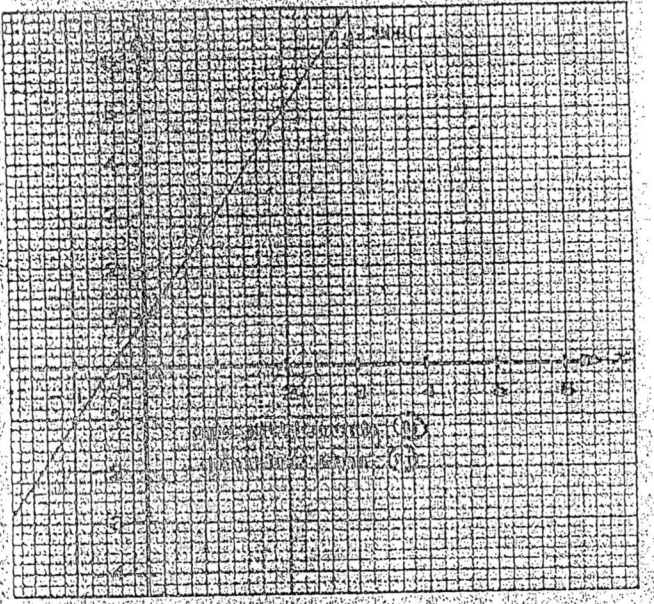
- (b) Solve these equations to find the value of one  $\bigcirc$ .

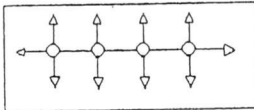
Answer (b) \_\_\_\_\_ [3]

Marking Scheme

|      |                                                                                                              |                                                                                |
|------|--------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------|
| 1(a) | $2500 = \frac{1}{d}$                                                                                         | B1                                                                             |
| 1(b) | $\frac{1}{40} = 0.025$                                                                                       | B1                                                                             |
| 2    | $\frac{58.4 \times 0.46}{13.2} \approx \frac{60 \times 0.5}{10}$<br>$= 3$                                    | M1<br>A1                                                                       |
| 3    | $\frac{2x+3}{3} - \frac{x}{2}$<br>$= \frac{2(2x+3) - 3(x)}{6}$<br>$= \frac{4x+6-3x}{6}$<br>$= \frac{x+6}{6}$ | M1<br>A1                                                                       |
| 4(a) | 30 mobile phones                                                                                             | B1                                                                             |
| 4(b) | January                                                                                                      | B1                                                                             |
| 5    | $p = \frac{3}{5}$<br>$q = 0.75$<br>$r = \frac{7}{5}$<br>$s = \frac{4}{2}$                                    | B1<br>B1<br>B1<br>B1                                                           |
| 6    |                           | B2 – for all lines drawn correctly<br>B1 – for 1 to 2 lines drawn incorrectly. |

|       |                                                                                                                                                                                                                                         |                |
|-------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------|
| 7(i)  | \$850 = ¥212 500                                                                                                                                                                                                                        | B1             |
| 7(ii) | Remaining ¥ = ¥212 500 - ¥24600 = ¥187 900<br><br>S\$1 = ¥260<br>S\$ x = ¥187 900<br>∴ x = S\$723(nearest dollar)                                                                                                                       | A1             |
| 8(a)  | 1 hour 25 minutes                                                                                                                                                                                                                       | B1             |
| 8(b)  | $Average Speed = \frac{15km}{1\frac{5}{12} hr}$ (ecf)<br>$= 10\frac{10}{17} km/h$ or $10.6 km/h$                                                                                                                                        | M1<br>A1       |
| 9(a)  | 8 months : 2 years 4 months<br>8 : 28<br>2 : 7                                                                                                                                                                                          | B1             |
| 9(b)  | $smaller amount = \frac{p}{p+q} \times 40$<br>$= \$ \frac{40p}{p+q}$                                                                                                                                                                    | M1<br>A1       |
| 10(a) | $sum of int \angle s = (n-2) \times 180^\circ$<br>$= (7-2) \times 180^\circ$<br>$= 900^\circ (shown)$                                                                                                                                   | B1             |
| 10(b) | $sum of int \angle s = 900^\circ$<br>$4(120) + x + (x+92) + (2x-20) = 900^\circ$<br>$552^\circ + 4x^\circ = 900^\circ$<br>$4x^\circ = 348^\circ$<br>$x^\circ = 87^\circ$<br>∴ largest $\angle = x + 92$<br>$= 87 + 92$<br>$= 179^\circ$ | M1<br>M1<br>A1 |
| 11(a) | Maximum waiting time = 61 mins                                                                                                                                                                                                          | B1             |
| 11(b) | Total no of patients = 17                                                                                                                                                                                                               | B1             |

|       |                                                                                                              |          |
|-------|--------------------------------------------------------------------------------------------------------------|----------|
| 11(c) | Modal waiting time = 30 minutes                                                                              | B1       |
| 12(a) | $x = -1, y = -1$<br>$x = 2, y = 5$                                                                           | B1<br>B1 |
| 12(b) |                             |          |
| 13(a) | $10x + 16x + 10x = 360$<br>$36x = 360$<br>$x = 10$                                                           | M1<br>A1 |
| 13(b) | $16x = 16(10) = 160$ (ecf)<br>$6x = 6(10) = 60$<br>Area of $\Delta = \frac{1}{2}(160)(60) = 4800\text{cm}^2$ | M1<br>A1 |
| 14(a) | $y = kx^2$<br>$27 = k(9)^2$<br>$k = \frac{27}{81} = \frac{1}{3}$<br>$y = \frac{1}{3}x^2$                     | M1<br>A1 |

|       |                                                                                                                       |                                                                                                                                                                    |                                                                                                     |              |
|-------|-----------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------|--------------|
| 14(b) | $\frac{1}{12} = \frac{1}{3}x^2$<br>$x^2 = \frac{1}{4}$<br>$x = \frac{1}{2}$ (ecf)                                     | A1                                                                                                                                                                 |                                                                                                     |              |
| 15(a) | $4^{-2} = \frac{1}{16} / 0.0625$                                                                                      | B1                                                                                                                                                                 |                                                                                                     |              |
| 15(b) | $27^{\frac{2}{3}} = 3^x$<br>$(3^3)^{\frac{2}{3}} = 3^x$<br>$3^2 = 3^x$<br>$x = 2$                                     | M1<br>A1                                                                                                                                                           |                                                                                                     |              |
| 16(a) | $x^2 - 4x + 7 = x^2 - 2px + q$<br>$\therefore -4 = -2p$<br>$p = 2$<br><br>$7 = p^2 + q$<br>$7 = (2)^2 + q$<br>$q = 3$ | B1<br><br><br>B1                                                                                                                                                   |                                                                                                     |              |
| 16(b) | <u>Hence (method)</u><br>$x^2 - 4x + 7 = 3$<br>$(x - 2)^2 + 3 = 3$<br>$(x - 2)^2 = 0$<br>$x = 2$                      | <u>Otherwise (method)</u><br>$x^2 - 4x + 7 = 3$<br>$x^2 - 4x + 4 = 0$<br>$a = 1, b = -4, c = 4$<br>$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(4)}}{2(1)}$<br>$x = 2$ | <u>Otherwise (method)</u><br>$x^2 - 4x + 7 = 3$<br>$x^2 - 4x + 4 = 0$<br>$(x - 2)^2 = 0$<br>$x = 2$ | M1<br><br>A1 |
| 17(a) | <br>Figure 4                     | B1                                                                                                                                                                 |                                                                                                     |              |
| 17(b) | Number of circles = 4<br>Number of triangles = 10                                                                     | B1 (award marks only when both answers correct)                                                                                                                    |                                                                                                     |              |

|           |                                                                                                                                                                           |          |
|-----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|
| 17(c)     | $Tn = a + (n-1)d$ $= 4 + (n-1)(2)$ $= 4 + 2n - 2$ $= 2 + 2n$                                                                                                              | M1<br>A1 |
| 18(a)     | $\angle AED = 78^\circ$ (opp $\angle$ s of $  $ -gram)                                                                                                                    | B1       |
| 18(b)     | $\angle DAE = 28^\circ$ (alt. $\angle$ s)                                                                                                                                 | B1       |
| 18(c)     | $\angle BAE = 180^\circ - 78^\circ$<br>$= 102^\circ$ (int $\angle$ s)                                                                                                     | B1       |
| 18(d)     | $\angle ACB = \frac{180^\circ - 78^\circ}{2} = 51^\circ$ (base $\angle$ s isos $\Delta$ )<br>$\angle ACD = 180^\circ - 51^\circ = 129^\circ$ (adj $\angle$ s on str line) | M1<br>A1 |
| 19(a)     | $P(\text{score of } 1) = \frac{3}{8}$                                                                                                                                     | B1       |
| 19(b)     | $P(\text{even no}) = \frac{3}{8}$                                                                                                                                         | B1       |
| 19(c)     | $P(\text{not a } 2) = \frac{6}{8} = \frac{3}{4}$                                                                                                                          | B1       |
| 20(a)     | Scale factor $= \frac{PT}{AE} = \frac{16.8}{4.2} = 4$                                                                                                                     | B1       |
| 20(b)     | $\angle RST = \angle CDE = 101^\circ$                                                                                                                                     | B1       |
| 20(c)     | $\frac{RS}{CD} = \frac{PT}{AE}$<br>$\frac{RS}{7} = \frac{4}{1}$<br>$RS = 2 \times 7 = 28 \text{ cm}$                                                                      | B1       |
| 21(a)     | Vol of brick $= 55 \times 30 \times 88$<br>$= 145\,200 \text{ cm}^3$                                                                                                      | A1       |
| 21(a)(ii) | Total SA $= 2(55 \times 30) + 2(30 \times 88) + 2(55 \times 88)$<br>$= 18\,260 \text{ cm}^2$                                                                              | M1<br>A1 |
| 21(b)     | Cost $= \$0.02 \times 18\,260 = \$365.20$ (ecf)                                                                                                                           | A1       |

|       |                                                                                                                                                                                                                                   |                                              |
|-------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------|
| 22(a) | $\frac{1}{4}x - 3 = 1$<br>$\frac{1}{4}x = 4$<br>$x = 16$                                                                                                                                                                          | A1                                           |
| 22(b) | $3(x-2)(x+4) = 0$<br>$x-2 = 0, x+4 = 0$<br>$x = 2, x = -4$                                                                                                                                                                        | B1, B1                                       |
| 22(c) | $3y^2 - 5y - 4 = 0$<br>$a = 3, b = -5, c = -4$<br>$y = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(3)(-4)}}{2(3)}$<br>$y = 2.26$ (2dp) $y = -0.59$ (2dp)                                                                                     | B1, B1<br>(-1 mark if answer is not in 2 dp) |
| 23(a) | gradient of BC $= \frac{y_2 - y_1}{x_2 - x_1}$<br>$= \frac{2 - 2}{5 - 1} = 0$                                                                                                                                                     | A1                                           |
| 23(b) | length of BC $= \sqrt{(5+1)^2 + (2+2)^2}$<br>$= \sqrt{52} = 7.21 \text{ units}$                                                                                                                                                   | A1                                           |
| 23(c) | Area of $\Delta ABC = \frac{1}{2}(4)(4)$<br>$= 8 \text{ units}^2$                                                                                                                                                                 | A1                                           |
| 23(d) | $D(3, -2)$                                                                                                                                                                                                                        | B1                                           |
| 24(a) | $2x + 3y = 78$<br>$x + y = 30$                                                                                                                                                                                                    | B1<br>B1                                     |
| 24(b) | $2x + 3y = 78$ --- eq1<br>$x + y = 30$ --- eq2<br><br>$eq2 \times 2: 2x + 2y = 60$ --- eq3<br>$2x + 3y = 78$ --- eq1<br>$eq3 - eq1: -y = -18$<br>$y = 18$<br>Subst into eq2: $x + 18 = 30$<br>$x = 12$<br>The value of $x$ is 12. | M1<br><br><br><br><br><br><br>M1<br><br>A1   |

Name: \_\_\_\_\_ ( )

Class: \_\_\_\_\_



GREENDALE SECONDARY SCHOOL  
End-of-Year Examination 2014

MATHEMATICS

4042/02

Paper 2

8 October 2014

Secondary Three Normal Academic

2 hours

Candidates answer on the Writing Paper.

READ THESE INSTRUCTIONS FIRST

Write your index number and name on all the work you hand in.  
Write in dark or blue pen.  
You may use a soft pencil for any diagrams or graphs.  
Do not use staples, paper clips, highlighters, glue or correction fluid.

Section A  
Answer all questions.

Section B  
Answer two questions.

If working is needed for any question it must be shown with the answer.  
Omission of essential working may result in loss of marks.  
You are expected to use a scientific calculator to evaluate explicit numerical expressions.  
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.  
For  $\pi$ , use either your calculator value or 3.142, unless the question required the answer in terms of  $\pi$ .

At the end of the examination, fasten all your work securely together.  
The number of marks is given in brackets [ ] at the end of each question or part question.  
The total number of marks for this paper is 60.

This document consists of 8 printed pages, including this cover page.

Greendale Secondary School 2014

Greendale Secondary School  
End-of-Year Examination 2014

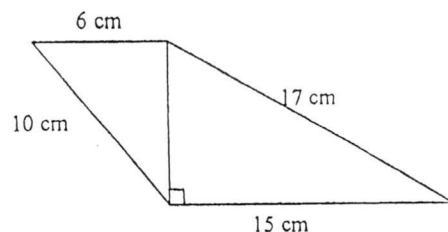
2

Secondary 3 Normal Academic  
Mathematics Paper 2

Section A  
Answer all the questions.

1. A car travelled for 3 hours 45 minutes at an average speed of 60 km/h.
  - (a) Express 3 hours 30 minutes in hours. [1]
  - (b) Find how far the car travelled. [1]Give your answer to the nearest kilometre.
2. The population of China is 3.67 billion.
  - (a) Write 3.67 billion in standard form. [1]
  - (b) Given that there are  $8 \times 10^5$  children, what fraction of the whole population are children? Give your answer in its simplest form. [1]
  - (c) The population doubles every 10 years.  
Find the population 40 years later.  
Write your answer in standard form. [2]
3.
  - (a) Write the highest common factor of 30 and 40. [2]
  - (b) The school bell in Spring School rings every 30 minutes while the school bell in Autumn School rings every 40 minutes. Both school bells ring at 8:15 am every day.  
At which time do both bells ring at the same time? [2]
4. Answer the whole of this question on the blank paper provided.  
In triangle  $ABC$ ,  $AB = 8$  cm,  $AC = 6$  cm and  $\angle BAC = 63^\circ$ .
  - (a) Construct an accurate drawing of triangle  $ABC$ . [2]
  - (b) Draw the angle bisector of  $\angle CBA$ . [2]
  - (c) The angle bisector  $\angle CBA$  meets  $AC$  at point  $P$ .  
Mark  $P$  on the drawing and write down the length of  $AP$ . [2]

5. In the diagram,  $\angle BAC = 90^\circ$ .  $AB = 15$  cm,  $BC = 17$  cm,  $AD = 10$  cm and  $CD = 6$  cm.



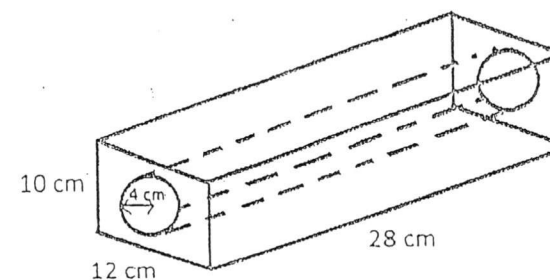
Find

- (a) the length of  $AC$ , [2]  
(b) Show that  $\angle ACD$  is a right angle. [2]
6. A survey conducted on 50 families in a block of flats regarding the number of children in each family is tabulated below.

| Number of children in the family | 0 | 1  | 2   | 3  | 4 |
|----------------------------------|---|----|-----|----|---|
| Frequency                        | 1 | 10 | $x$ | 16 | 5 |

- (a) Find the value of  $x$ , [1]  
(b) Find the mean number of children in a family. [3]  
(c) If the results of the survey were represented by a pie chart, calculate the angle of the sector representing 3 children in the family. [2]

7. The diagram shows a solid formed by removing a cylinder from a rectangular cuboid.



- (a) Given that the radius of cylinder is 4 cm, calculate the volume of the solid. [4]  
(b) The solid is made from a material with density  $1.1 \text{ g/cm}^3$ . Calculate the mass of the solid. [2]
8. (a) Peter sold his stamp collection for \$12 000. He made a profit of 20% on what he paid for. How much did he pay for his stamp collection. [2]  
(b) Peter saved the \$12 000 in a bank at 4.8% per year simple interest. What was the value of his savings after 3 years? [3]  
(c) Which was greater, the profit he made on the stamp collection or the interest in 3 years from the bank, and by how much? [2]
9. (a) Factorise completely  $2x^2 - 50$ . [2]  
(b) Express as a single denominator  $\frac{2x}{3} - \frac{3(x-2)}{5}$ . [2]  
(c) Simplify fully  $\frac{3b^2}{4} + \frac{12b}{5c}$ . [1]

## Section B

Answer any two questions. Each question carries 8 marks.

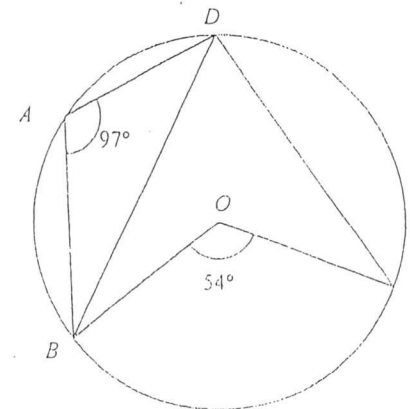
10. Answer the whole of this question on a single sheet of graph paper.

The table below is for  $y = x^3 - 6x^2 + 3x + 11$ .

|     |     |    |    |   |   |    |     |
|-----|-----|----|----|---|---|----|-----|
| $x$ | -2  | -1 | 0  | 1 | 2 | 4  | 6   |
| $y$ | -27 | 1  | 11 | 9 | 1 | -9 | $q$ |

- (a) Calculate the value of  $q$ . [1]
- (b) Using a scale of 2 cm to 1 unit, draw a horizontal  $x$ -axis of  $-2 \leq x \leq 6$ .  
Using a scale of 2 cm to 10 units, draw a vertical  $y$ -axis of  $-30 \leq y \leq 30$ .  
Plot the graph of  $y = x^3 - 6x^2 + 3x + 11$  for  $-2 \leq x \leq 6$ . [3]
- (c) Find the values of  $x$  when  $y = 0$ . [2]
- (d) By drawing a tangent, find the gradient of the curve at  $x = 3$ . [2]

11. (a)



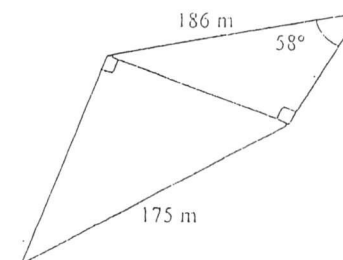
$A, B, C$  and  $D$  are points on a circle with centre  $O$ .  
 $\angle BOC = 54^\circ$  and  $\angle BAD = 97^\circ$ .

Find

- (i)  $\angle BDC$ , [1]  
(ii)  $\angle BCD$ , [1]  
(iii)  $\angle OCD$ . [2]

- (b) The figure shows some footpaths in a park.

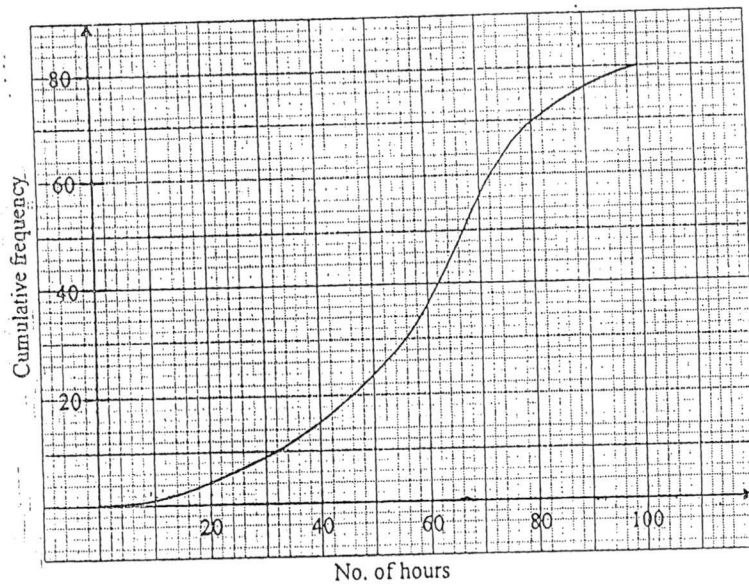
$AB = 175$  m, path  $DC = 186$  m,  $\angle BCD = 58^\circ$ ,  $\angle ADB = \angle DBC = 90^\circ$ .



Find

- (i) the length of path  $DB$ . [2]  
(ii)  $\angle ABD$ . [2]

12. (a) The cumulative frequency curve below illustrates the number of hours spent by 80 students to prepare for their Sports Day.

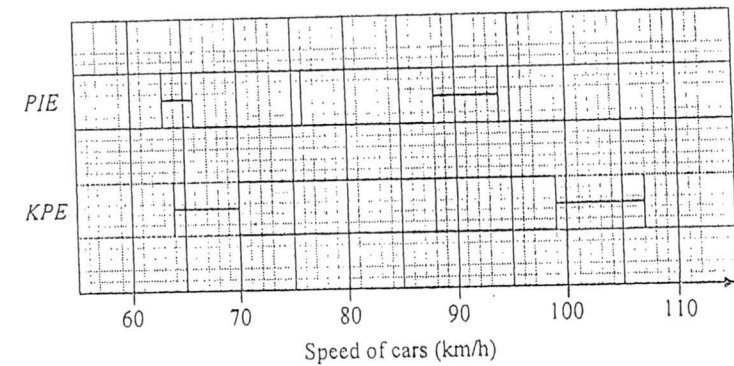


Use the graph to find

- the median number of hours spent on preparing for Sports Day. [1]
- the interquartile range. [2]
- Given that 12.5% of students spend at least  $x$  hours preparing for Sports Day, find the value of  $x$ . [1]

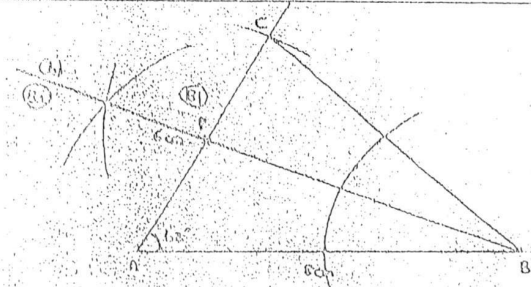
- (b) The speeds of cars crossing a checkpoint along Pan Island Expressway (PIE) and Kallang Paya Lebar Expressway (KPE) were recorded.

The results are summarised in the box-and-whisker plots below.



- Write down the median speed of the cars at PIE. [1]
- At which expressway do the cars travel at a faster speed? Give a reason for your answer. [1]
- Find the interquartile range of the speed of the cars at KPE. [1]
- At which expressway do the cars travel at a more consistent speed. Give a reason for your answer. [1]

Marking Scheme (Paper 2)

|      |                                                                                                                                                                                                                                       |          |
|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|
| 1(a) | $3\text{hrs } 30\text{mins} = 3\frac{1}{2}\text{ hr} / 3.5\text{hours}$                                                                                                                                                               | B1       |
| 1(b) | $\text{distance} = \text{speed} \times \text{time}$ $= 60 \times 3\frac{1}{2}$ $= 210\text{ km}$                                                                                                                                      | A1       |
| 2(a) | $3.67\text{ billion} = 3.67 \times 10^9$                                                                                                                                                                                              | B1       |
| 2(b) | $\text{fraction} = \frac{8 \times 10^5}{3.67 \times 10^9}$ $= \frac{2}{9175}$                                                                                                                                                         | M1<br>A1 |
| 2(c) | $\text{Population} = 2^4 \times 3.67 \times 10^9$ $= 5.872 \times 10^{10}\text{ people}$                                                                                                                                              | M1<br>A1 |
| 3(a) | $\text{HCF} = 2 \times 5$ $= 10$                                                                                                                                                                                                      | M1<br>A1 |
| 3(b) | $\text{LCM} = 2 \times 5 \times 3 \times 4$ $= 120\text{ min s}$<br>$120\text{ min s} = 2\text{hours}$ $\text{Next time flash together} = 10:15\text{am}$                                                                             | M1<br>A1 |
| 4    |  <p>(a) accurate drawing (A1)<br/>         construction arcs &amp; labelling (A1)<br/>         (b) on diagram (A1)<br/>         total: 6 marks</p> |          |

|      |                                                                                                                                                                                                                                                                      |                      |
|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------|
| 5(a) | <p>Pythagoras theorem</p> $17^2 = AC^2 + 15^2$ $AC^2 = 64$ $AC = 8$                                                                                                                                                                                                  | M1<br>A1             |
| 5(b) | $10^2 = 100$ $8^2 + 6^2 = 100$ $\therefore 10^2 = 8^2 + 6^2$ $\therefore \text{by converse of Pythagoras Thm,}$ $\angle ACD = 90^\circ$                                                                                                                              | M1<br>A1             |
| 6(a) | $1 + 10 + x + 16 + 5 = 50$ $32 + x = 50$ $x = 18$                                                                                                                                                                                                                    | A1                   |
| 6(b) | $\text{mean} = \frac{0(1) + 1(10) + 2(18) + 3(16) + 4(5)}{50}$ $= \frac{114}{50}$ $= 2.28\text{ children} / 2\frac{7}{25}\text{ children}$                                                                                                                           | M1<br>M1<br>A1       |
| 6(c) | $\text{Angle rep 3children} = \frac{16}{50} \times 360^\circ$ $= 115.2^\circ$                                                                                                                                                                                        | M1<br>A1             |
| 7(a) | $\text{Vol of cuboid} = 10 \times 12 \times 28$ $= 3360\text{ cm}^3$ $\text{Vol of cylinder} = \pi r^2 h$ $= 3.142 \times 4^2 \times 28$ $= 1407.616\text{ cm}^3$ $\text{Vol of solid} = 3360 - 1407.616$ $= 1952.384\text{ cm}^3$ $= 1950\text{ cm}^3\text{ (3sf)}$ | M1<br>M1<br>M1<br>A1 |
| 7(b) | $\text{mass} = \text{Vol} \times \text{Density}$ $= 1952.384 \times 1.1\text{ (ecf)}$ $= 2147.6224\text{g}$ $= 2150\text{g (3sf)}$                                                                                                                                   | M1<br>A1             |

|        |                                                                                                                                                    |                |
|--------|----------------------------------------------------------------------------------------------------------------------------------------------------|----------------|
| B(a)   | $120\% \rightarrow \$12000$<br>$100\% \rightarrow \$\left(\frac{12000}{120} \times 100\right)$<br>$= \$10000$                                      | M1<br>A1       |
| B(b)   | $I = \frac{PRT}{100}$<br>$= \frac{12000 \times 4.8 \times 3}{100}$<br>$= \$1728$<br>$\text{total savings} = \$12000 + \$1728$<br>$= \$13728$       | M1<br>M1<br>A1 |
| B(c)   | $\text{profit} = \$2000$<br>$\text{interest} = \$1728$<br>$\text{Increase} = \$2000 - \$1728 = \$272$<br>$\text{The profit is greater by } \$272.$ | B1<br>B1       |
| 3(a)   | $2x^2 - 50$<br>$= 2(x^2 - 25)$<br>$= 2(x^2 - 5^2)$<br>$= 2(x+5)(x-5)$                                                                              | M1<br>A1       |
| 3(bi)  | $\frac{2x}{3} - \frac{3(x-2)}{5}$<br>$= \frac{5(2x) - 9(x-2)}{15}$<br>$= \frac{10x - 9x + 18}{15}$<br>$= \frac{x+18}{15}$                          | M1<br>A1       |
| 3(bii) | $\frac{3b^2}{4} + \frac{12b}{5c}$<br>$= \frac{3b^2}{4} \times \frac{5c}{12b}$<br>$= \frac{5bc}{16}$                                                | B1             |

|          |                                                                                                                                                         |          |
|----------|---------------------------------------------------------------------------------------------------------------------------------------------------------|----------|
|          | Section B                                                                                                                                               |          |
| 10       | On graph paper – Refer to attached.                                                                                                                     |          |
| 11(i)    | $\angle BDC = \frac{54^\circ}{2}$ ( $\angle$ at centre = 2 $\angle$ at circumference)<br>$= 27^\circ$                                                   | B1       |
| 11(ii)   | $\angle BCD = 180^\circ - 97^\circ$<br>$= 83^\circ$ (opp $\angle$ s of cyclic quad)                                                                     | B1       |
| 11(iii)  | $\angle OCB = \frac{180^\circ - 54^\circ}{2}$<br>$= 63^\circ$ (base $\angle$ s of isos $\Delta$ )<br>$\angle OCD = 83^\circ - 63^\circ$<br>$= 20^\circ$ | M1<br>A1 |
| 11(bi)   | $\sin 58^\circ = \frac{DB}{186}$<br>$DB = 186 \sin 58^\circ$<br>$= 157.7369459$<br>$\approx 158 \text{ m}$                                              | M1<br>A1 |
| 11(bii)  | $\cos ABD = \frac{157.7369459}{175}$<br>$\angle ABD = 25.6633839^\circ$<br>$\approx 25.7^\circ$ (1 dp)                                                  | M1<br>A1 |
| 12(ai)   | median = 62 hours                                                                                                                                       | B1       |
| (a ii)   | $Q_1 = 46 \text{ hrs}$<br>$Q_3 = 72 \text{ hrs}$<br>$\text{interquartile range} = Q_3 - Q_1$<br>$= 72 - 46$<br>$= 26 \text{ hrs}$                       | M1<br>A1 |
| (a i ii) | $12.5\% \times 80 = 10 \text{ students}$<br>$\therefore x = 32 \text{ hrs}$                                                                             | A1       |

|        |                                                                                                                                               |    |
|--------|-----------------------------------------------------------------------------------------------------------------------------------------------|----|
| 12(bi) | Median (PIE) = 76 km/h                                                                                                                        | B1 |
| (bii)  | Median (KPE) = 88 km/h<br>Cars travel at higher speeds at KPE; because it has a higher median speeds as compared to speeds on PIE.            | B1 |
| (biii) | $Q_1 = 70 \text{ hrs}$<br>$Q_3 = 99 \text{ hrs}$<br>$IQR(KPE) = Q_3 - Q_1$<br>$= 99 - 70$<br>$= 29 \text{ km/h}$                              | B1 |
| (biv)  | $IQR(PIE) = Q_3 - Q_1$<br>$= 88 - 66$<br>$= 22 \text{ km/h}$<br>Cars travel with a more consistent speed at PIE because it has a smaller IQR. | B1 |

